

# Pharmacokinetic and Statistical Analysis of BE Data

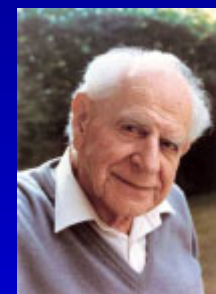
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BEBAC

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# To bear in Remembrance...

Whenever a theory appears to you as the only possible one, take this as a sign that you have neither understood the theory nor the problem which it was intended to solve.

**Karl R. Popper**



Even though it's *applied* science we're dealin' with, it still is – *science!*

**Leslie Z. Benet**



# NCA vs. PK Modeling

- Pharmacokinetic models

- Useful for understanding the drug/formulation

- Study design of BA/BE, e.g.,  
washout, accumulation / saturation to steady state

- Drawbacks

- Almost impossible to validate (fine-tuning of side conditions, weighting schemes, software, ...)
    - Still a mixture of art and science
    - Impossible to recalculate any given dataset using different software – sometimes even different versions of the same software!
    - Not acceptable for *evaluation* of BE studies!

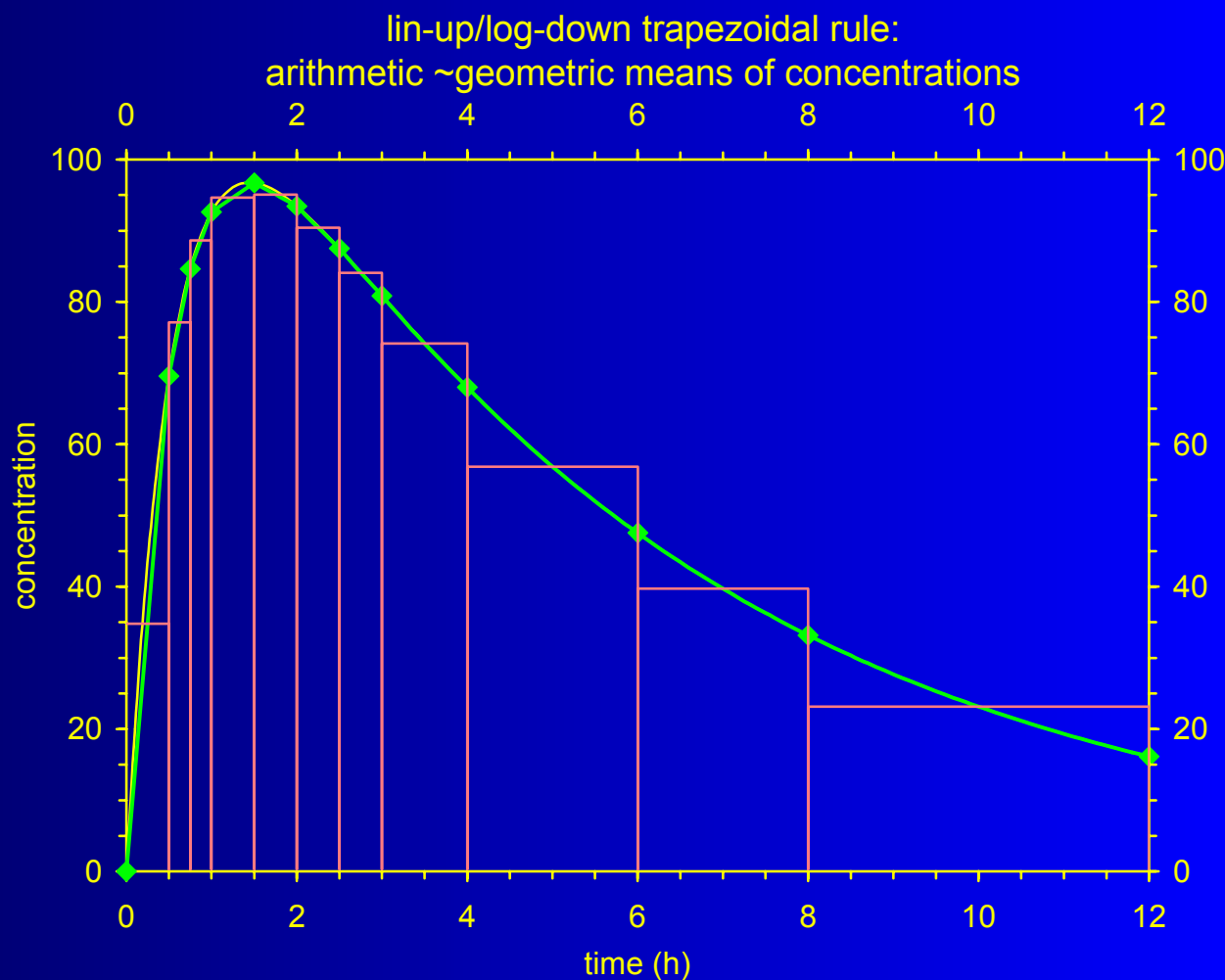
# NCA: Single Dose

- Noncompartmental methods do not rely on a PK (=compartmental) model
- Also known as SHAM (**S**hape, **H**eight, **A**rea, **M**oments)
  - Metrics (plasma, single dose)
    - Extent of absorption (EU...), total exposure (US):  $AUC$  (Area Under the Curve)
    - Rate of absorption (EU...), peak exposure (US):  $C_{max}$
    - $t_{max}$  (EU...)
    - Early exposure (US, CAN):  $pAUC_{t_{max}}$ ; AUC truncated at population's (CAN: subject's)  $t_{max}$  of the reference
    - Others:  $C_{min}$ , **Fluctuation**, **MRT**, **Occupancy time**,  $t_{lag}$ , ...

# NCA: AUC

- Recommended: lin-up/log-down trapezoidal rule
  - Hybrid of linear and log-linear
  - Sections with *increasing or equal* concentrations ( $C_{i+1} \geq C_i$ ) calculated by **linear trapezoidal** rule
  - Sections with *decreasing* concentrations ( $C_{i+1} < C_i$ ) calculated by **log-linear** trapezoidal rule
  - Avoids bias in both absorption and distribution/elimination phases
  - Suitable for IV and EV
  - Suitable for multiphasic profiles

# NCA: AUC





# NCA: AUC Extrapolation

## ● $AUC_{0-\infty}$

- Unweighted log-linear regression of  $\geq 3$  data points in the elimination phase
- Don't rely on softwares' automatic methods; visual inspection of the fit mandatory
- Extrapolation from  $AUC_{0-t}$  (regardless the method)

$$AUC_{\infty} = AUC_t + \frac{C_t}{\hat{\lambda}_z} \quad \text{or better} \quad AUC_{\infty} = AUC_t + \frac{\hat{C}_t}{\hat{\lambda}_z}$$

# NCA: other PK Metrics

## ● Single dose

- $C_{max}$  and  $t_{max}$  directly from profile
- Metrics describing the shape of the profile
  - Early exposure (US, CAN):  $AUC_{t_{max}} = pAUC$  truncated at population (CAN: subject's)  $t_{max}$  of the reference
  - Biphasic MR formulations:  $pAUCs$  truncated at a prespecified cut-off time point
    - FDA: Product specific guidances (methylphenidate, zolpidem)
    - EMA: All products

*Questions & Answers: Positions on specific questions addressed to the pharmacokinetics working party*

EMA/618604/2008 Rev. 7 (13 February 2013)

[http://www.ema.europa.eu/docs/en\\_GB/document\\_library/Scientific\\_guideline/2009/09/WC50002963.pdf](http://www.ema.europa.eu/docs/en_GB/document_library/Scientific_guideline/2009/09/WC50002963.pdf)



# NCA: other PK Metrics

- Single dose

- Metrics describing the shape of the profile

- $C_{max}/AUC$

- $t_{75\%} = POT-75$  (Plateau time, Peak-Occupancy-Time 75: time interval where  $C(t) \geq 75\%$  of  $C_{max}$ )

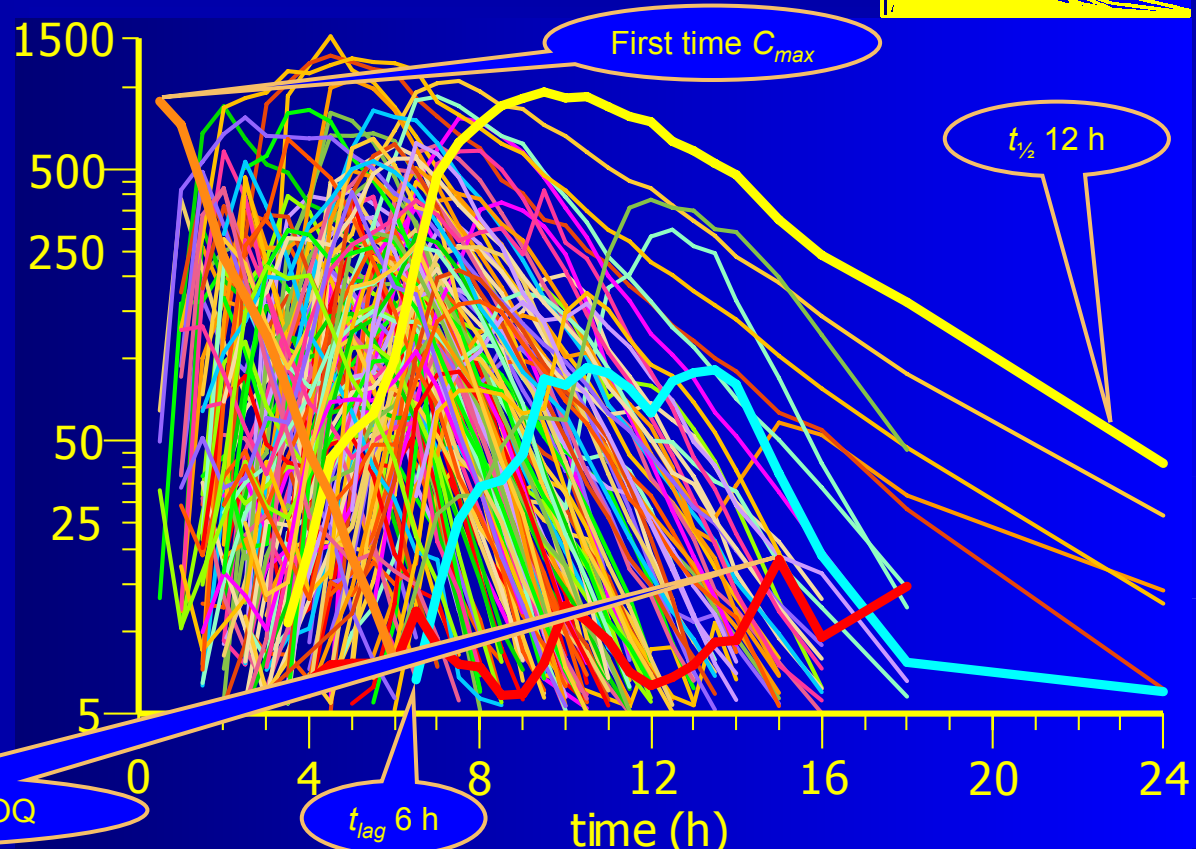
- $HVD = POT-50$  (Half Value Duration, Peak-Occupancy-Time 50: time interval where  $C(t) \geq 50\%$  of  $C_{max}$ )

- Occupancy time,  $t \geq MIC$  (time interval where  $C(t)$  is above some limiting concentration)

# Case Study (PPI)

- Attempt to deal with high variability

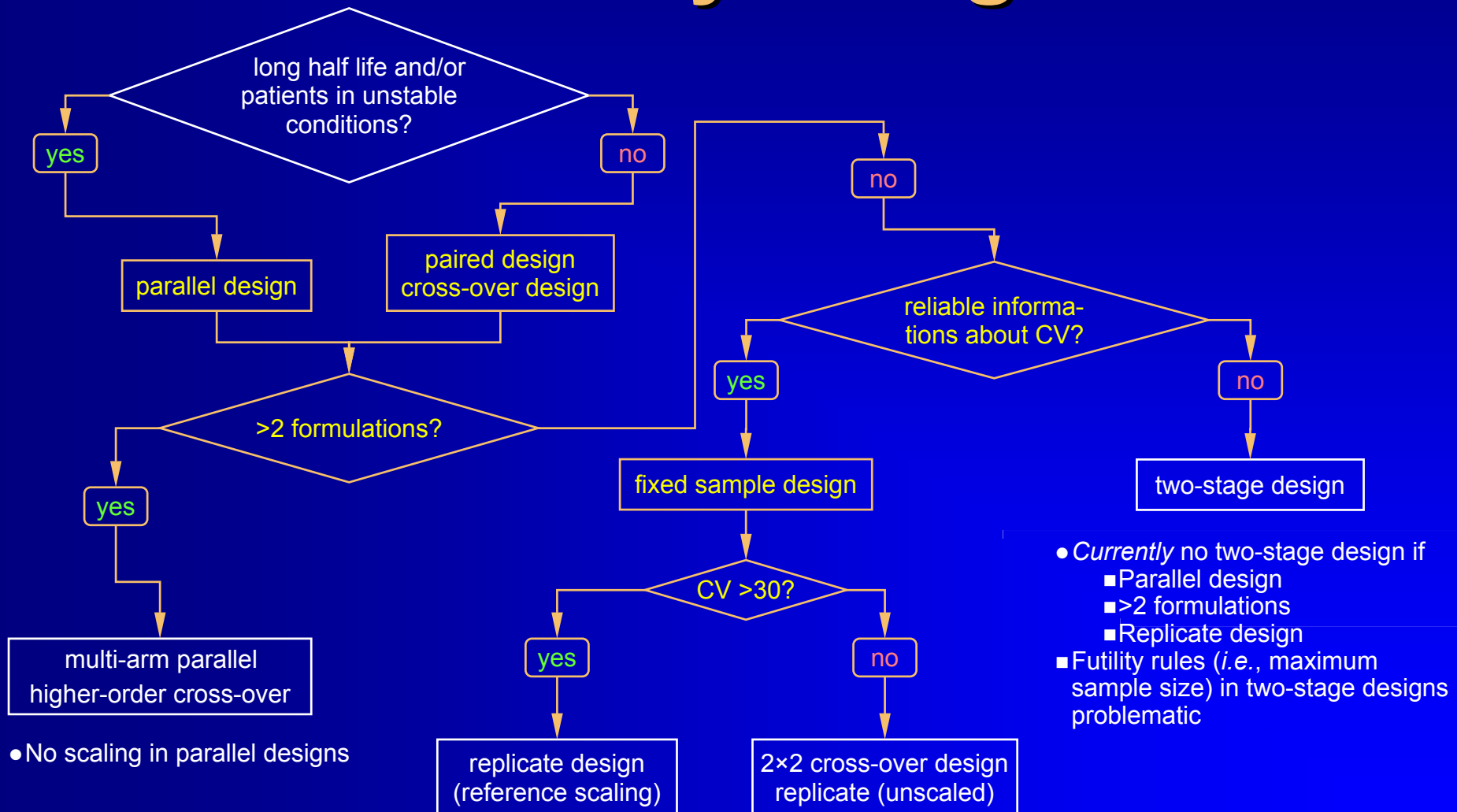
Powered to 90% according to CV from previous studies; 140 (!) subjects and to 80% for expected dropout rate. Sampling every 30 min up to 14 hours (7,785 total)



# NCA: Multiple Dose

- $AUC_{\tau}$  (dosage interval  $\tau$ ) or  $AUC_{ss,24h}$  (if more than o.a.d. and chronopharmacological variation)
- No extrapolation!
- $C_{ss,max}$  and  $C_{ss,min}$  directly from profile
- Peak-Trough-Fluctuation:  $(C_{ss,max} - C_{ss,min}) / C_{ss,av}$ , where  $C_{ss,av} = AUC_{\tau} / \tau$
- Swing:  $(C_{ss,max} - C_{ss,min}) / C_{ss,min}$

# BE Study Designs



# BE Study Designs

- The more 'sophisticated' a design is, the more information can be extracted

- Hierarchy of designs:

Full replicate (TRTR | RTRT or TRT | RTR), ↗

Partial replicate (TRR | RTR | RRT) ↗

Standard 2×2 cross-over (RT | RT) ↗

Parallel (R | T)

- Variances which can be estimated:

Parallel: total variance (between + within)

2×2 Xover: + between, within subjects ↗

Partial replicate: + within subjects (reference) ↗

Full replicate: + within subjects (reference, test) ↗



# Data Transformation?

- BE testing started in the early 1980s with an acceptance range of 80% – 120% of the reference based on the *normal* distribution
- Was questioned in the mid 1980s
  - Like many biological variables *AUC* and *C<sub>max</sub>* do not follow a normal distribution
    - Negative values are impossible
    - The distribution is skewed to the right
    - Might follow a *lognormal* distribution
  - Serial dilutions in bioanalytics lead to multiplicative errors

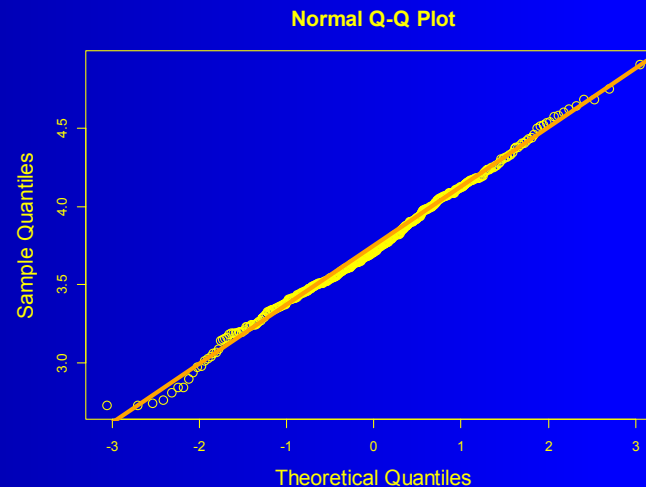
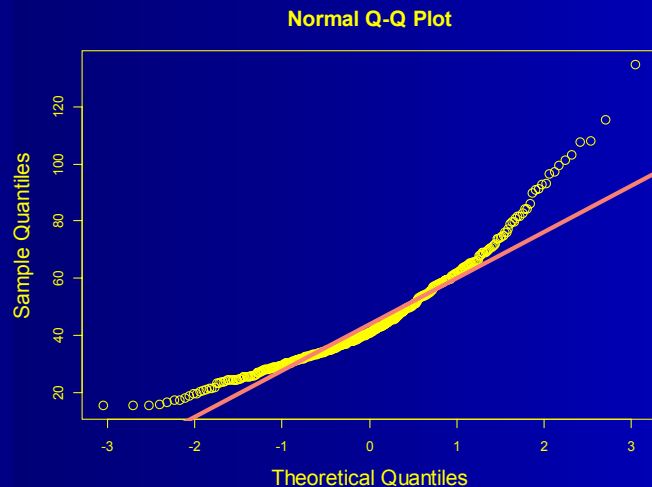
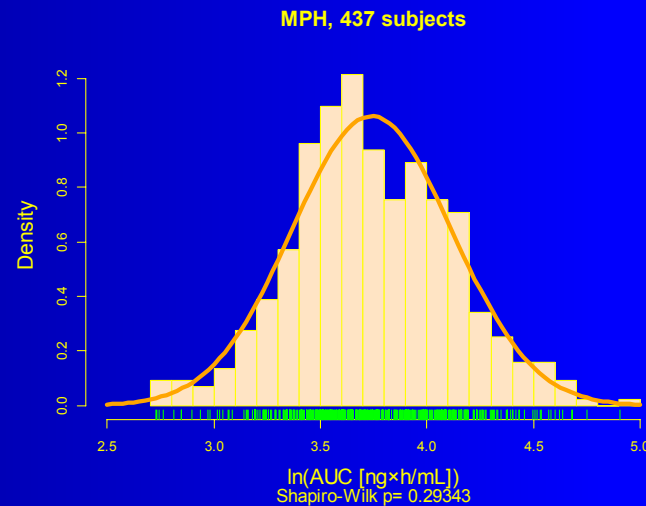
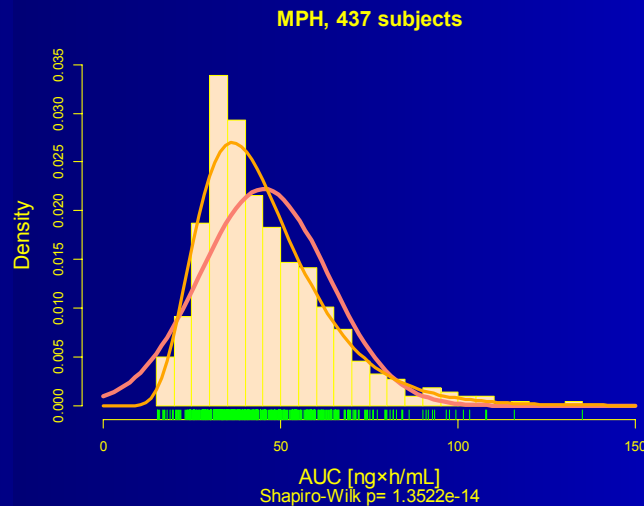


# Data Transformation?

Pooled data from real studies.

Clearly in favor of a lognormal distribution.

Shapiro-Wilk test highly significant for normal distribution (assumption rejected).



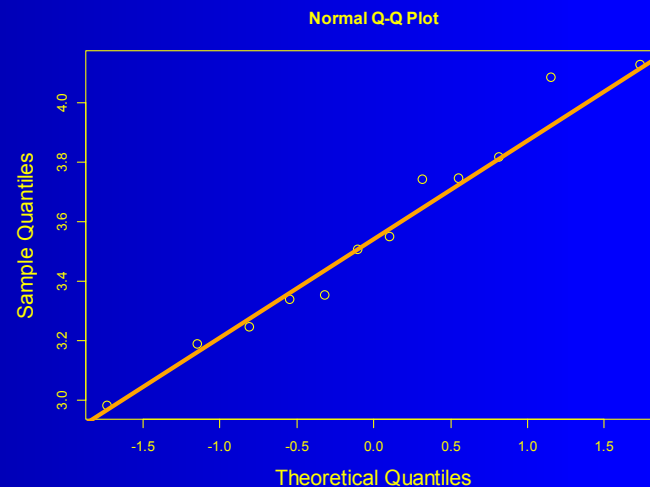
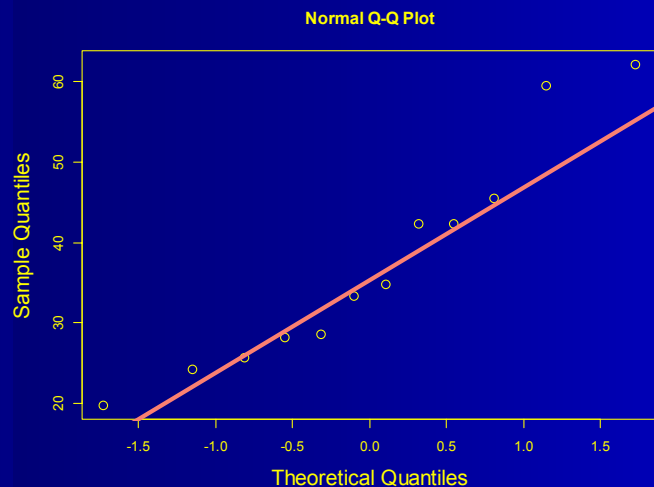
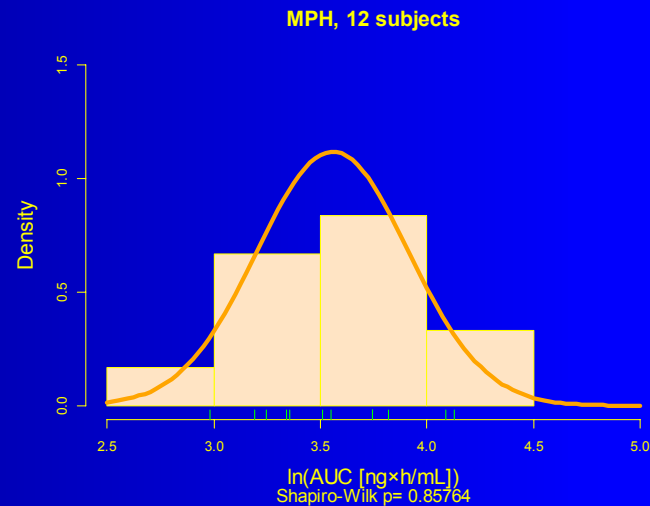
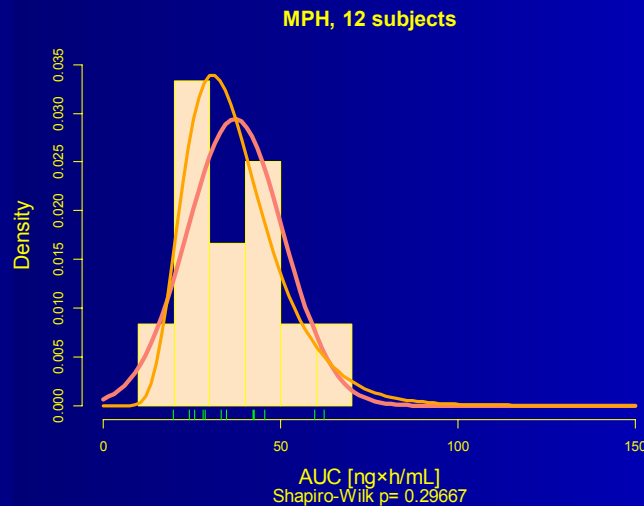
# Data Transformation!

Data of a real study.

Both tests *not* significant (assumptions accepted).

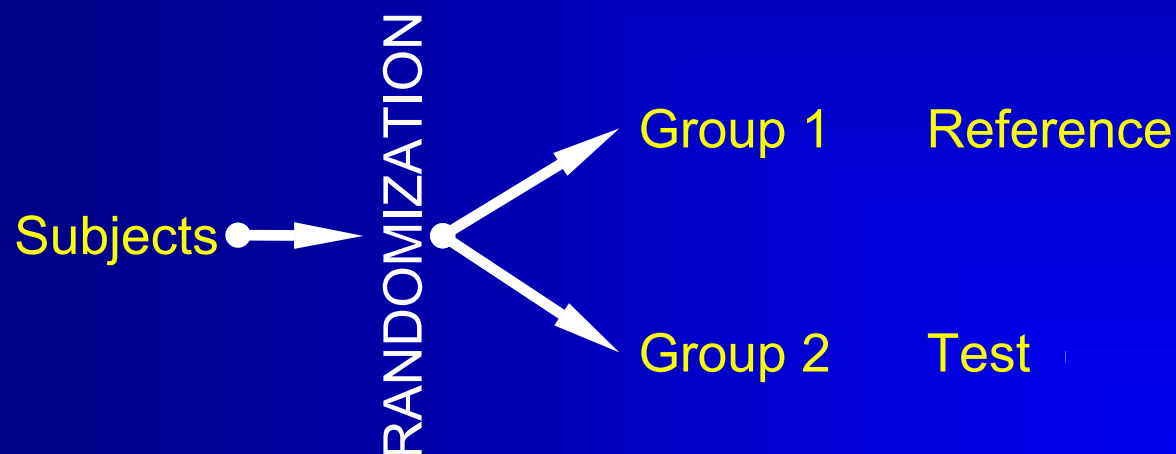
Tests not acceptable according to GLs.

Transformation based on prior knowledge (PK)!



# Parallel designs

- Two-Group Parallel Design



# Parallel designs (cont'd)

- Two-group parallel design

- Advantages

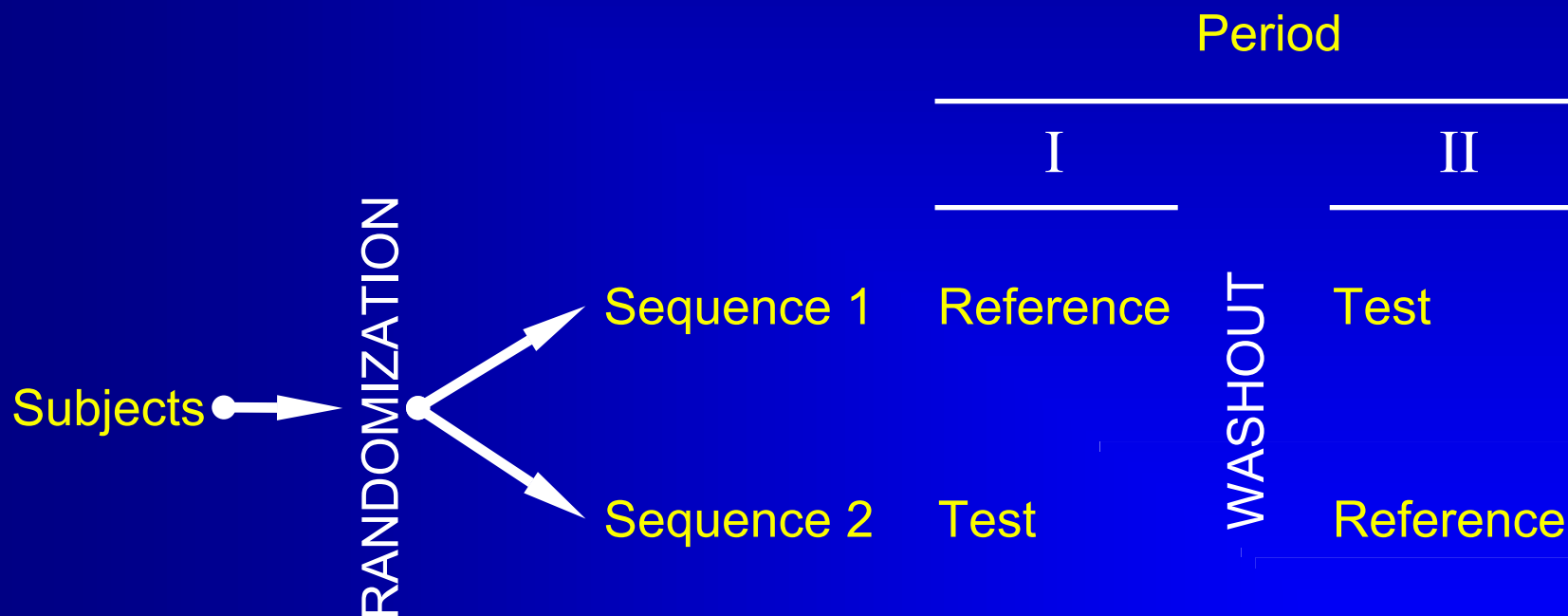
- Clinical part – *sometimes* – faster than X-over.
    - Straightforward statistical analysis.
    - Drugs with long half life.
    - Potentially toxic drugs or effect and/or AEs unacceptable in healthy subjects.
    - Studies in patients, where the condition of the disease irreversibly changes.

- Disadvantages

- Lower statistical power than X-over (*rule of thumb*: sample size should at least be doubled).
    - Phenotyping mandatory for drugs showing polymorphism.

# Cross-over designs

- Standard 2×2×2 Design



# Cross-over designs (cont'd)

- Every subject is treated both with test and reference
- Subjects are randomized into two groups; one is receiving the formulations in the order RT and the other one in the order TR. These two orders are called **sequences**
- Whilst in a paired design we must rely on the assumption that no external influences affect the periods, a cross-over design will account for that





# Cross-over design: Model

Multiplicative Model (X-over without carryover)

$$\ln(X_{ijk}) = \ln(\mu) + \ln(\pi_k) + \ln(\Phi_l) + \ln(s_{ik}) + \ln(e_{ijk})$$

$$X_{ijk} = \mu \cdot \pi_k \cdot \Phi_l \cdot s_{ik} \cdot e_{ijk}$$

$X_{ijk}$ : response of  $j$ -th subject ( $j=1, \dots, n_i$ ) in  $i$ -th sequence ( $i=1, 2$ ) and  $k$ -th period ( $k=1, 2$ ),  $\mu$ : global mean,  $\mu_l$ : expected formulation means ( $l=1, 2$ :  $\mu_1 = \mu_{test}$ ,  $\mu_2 = \mu_{ref.}$ ),  $\pi_k$ : fixed period effects,  $\Phi_l$ : fixed formulation effects ( $l=1, 2$ :  $\Phi_1 = \Phi_{test}$ ,  $\Phi_2 = \Phi_{ref.}$ )

# Cross-over design: Assumptions

## Multiplicative Model (X-over without carryover)

$$X_{ijk} = \mu \cdot \pi_k \cdot \Phi_l \cdot s_{ik} \cdot e_{ijk}$$

- All  $\ln\{s_{ik}\}$  and  $\ln\{e_{ijk}\}$  are independently and normally distributed about unity with variances  $\sigma_s^2$  and  $\sigma_e^2$ .
  - ➔ This assumption may not hold true for all formulations; if the reference formulation shows higher variability than the test formulation, a 'good' test will be penalized for the 'bad' reference.
- All observations made on different subjects are independent.
  - ➔ This assumption should not be a problem, unless you plan to include twins or triplets in your study...



# Cross-over designs (cont'd)

- Standard  $2 \times 2 \times 2$  design

- Advantages

- Globally applied standard protocol for bioequivalence, PK interaction, food studies
    - Straightforward statistical analysis

- Disadvantages

- Not suitable for drugs with long half life (→ parallel groups)
    - Not optimal for studies in patients with instable diseases (→ parallel groups)
    - Not optimal for HVDs/HVDPs (→ Replicate Designs)



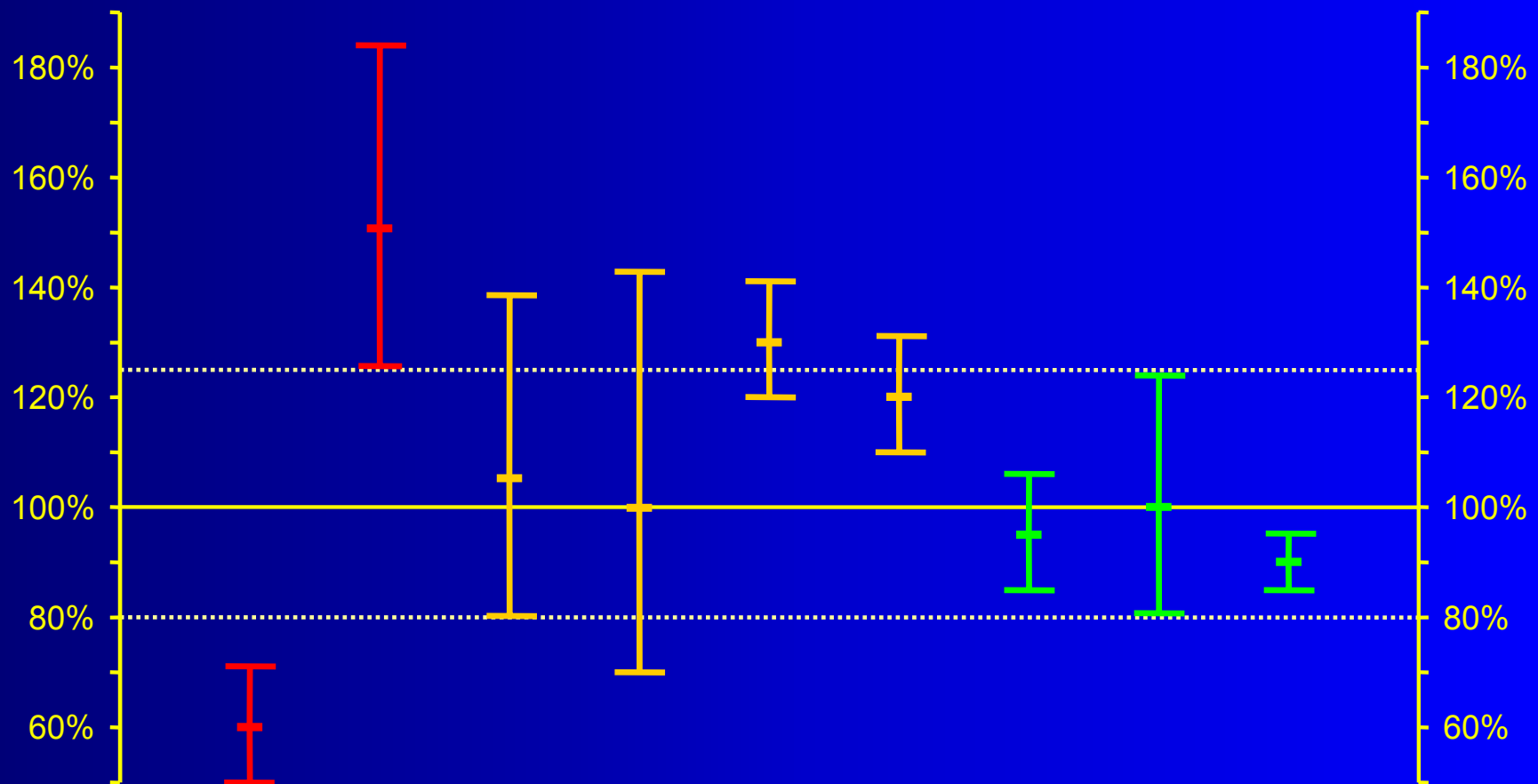
# BE Evaluation

- Based on the design set up a statistical model.
- Calculate the test/reference ratio.
- Calculate the 90% confidence interval (CI) around the ratio.
- The *width* of the CI depends on the variability observed in the study.
- The *location* of the CI depends on the observed test/reference-ratio.

# BE Assessment

- Decision rules based on the CI and the Acceptance Range (AR)
  - CI *entirely outside* the AR:  
Bioinequivalence proven
  - CI *overlaps* the AR (lies *not entirely within* the AR):  
Bioequivalence not proven – indecisive
  - CI lies *entirely within* the AR:  
Bioequivalence proven

# BE Assessment





# Add-on / Two-Stage Designs

- Sometimes properly designed and executed studies fail due to
  - 'true' bioinequivalence,
  - poor study conduct (increasing variability),
  - pure chance (producer's risk hit),
  - false (over-optimistic) assumptions about variability and/or T/R-ratio.
- The patient's risk must be preserved
  - Already noticed at Bio-International Conferences (1989, 1992) and guidelines from the 1990s.

# Sequential Designs

- Have a long and accepted tradition in clinical research (mainly phase III)
  - Based on work by Armitage *et al.* (1969), McPherson (1974), Pocock (1977), O'Brien and Fleming (1979), Lan & DeMets (1983), ...
    - First proposal by Gould (1995) in the area of BE did not get regulatory acceptance in Europe, but
    - new methods stated in recent guidelines.

## AL Gould

*Group Sequential Extension of a Standard Bioequivalence Testing Procedure*  
J Pharmacokin Biopharm 23(1), 57–86 (1995)

# Sequential Designs

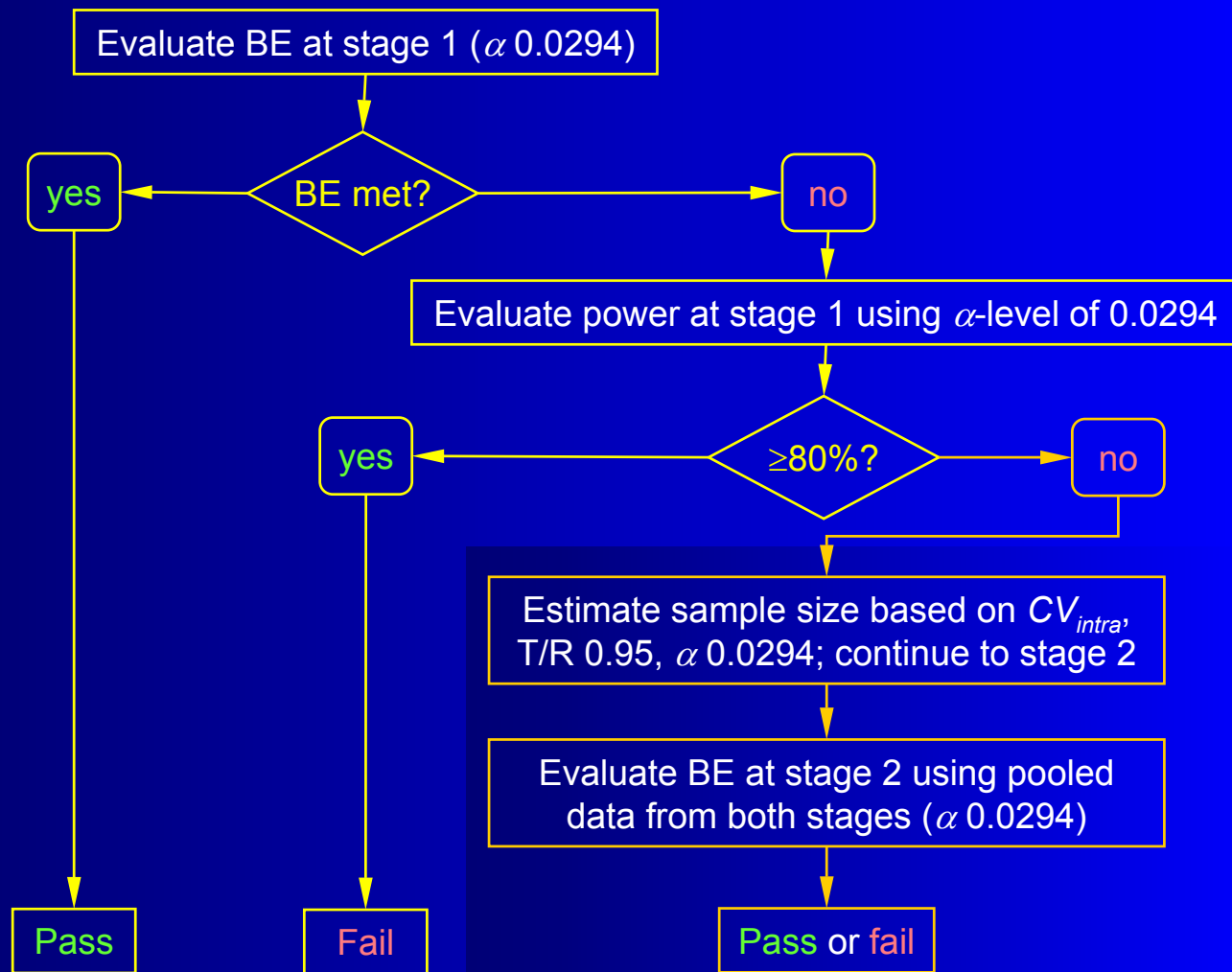
- Methods by Potvin *et al.* (2008) first validated framework in the context of BE
  - Supported by the 'Product Quality Research Institute' (members: FDA/CDER, Health Canada, USP, AAPS, PhRMA...)
    - Three of BEBAC's protocols accepted by German BfArM, one product approved in 06/2011.

Potvin D, Diliberti CE, Hauck WW, Parr AF, Schuirmann DJ, and RA Smith  
*Sequential design approaches for bioequivalence studies with crossover designs*  
Pharmaceut Statist 7(4), 245–62 (2008) [DOI: 10.1002/pst.294](https://doi.org/10.1002/pst.294)

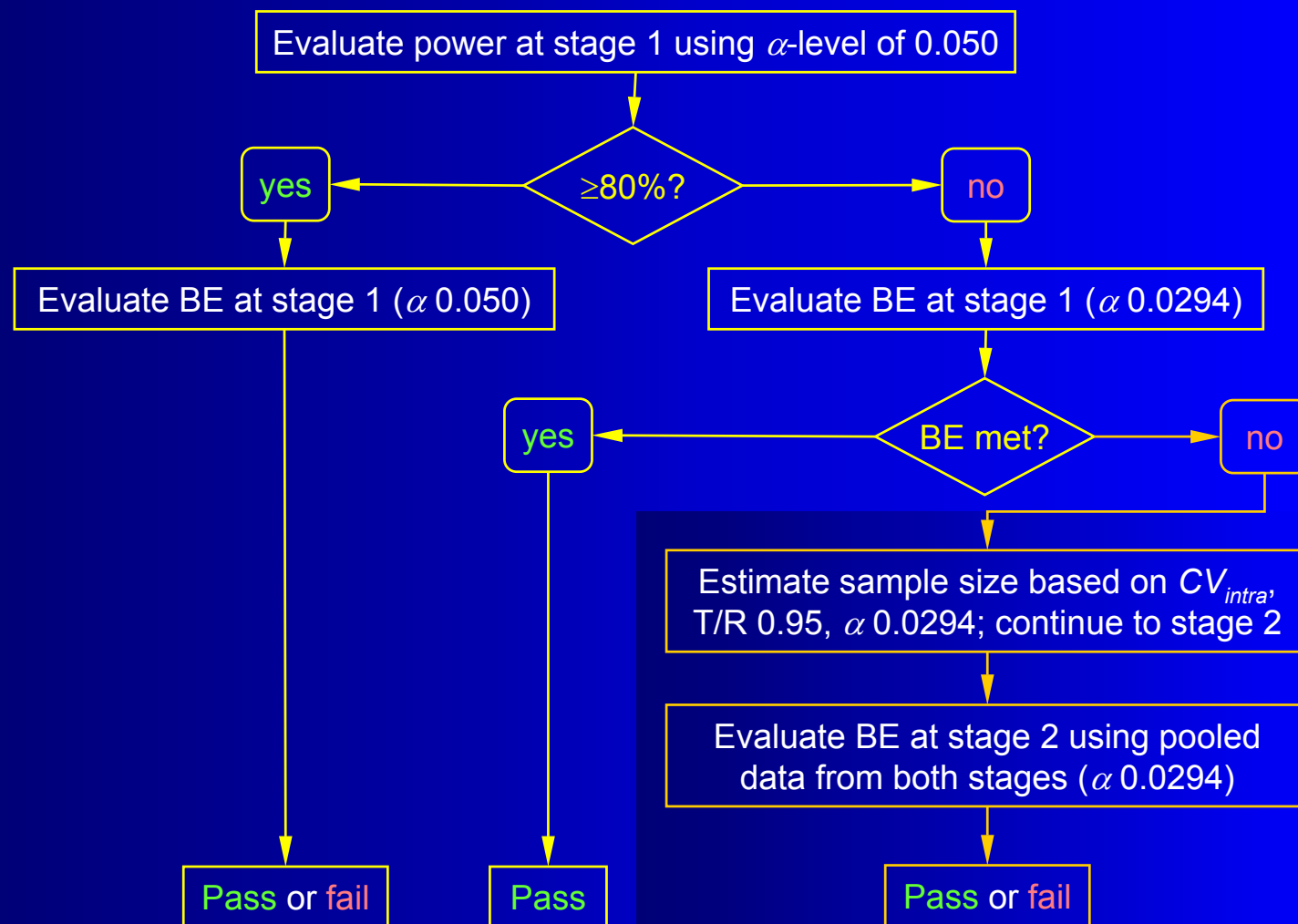
# Review of Guidelines

- EMA (Jan 2010)  
Acceptable; Potvin *et al.* Method B preferred (?)
- Russia (Draft 2011)  
Acceptable (Methods B and C)
- Canada (May 2012)  
Potvin *et al.* Method C recommended
- FDA (Jun 2012)  
Potvin *et al.* Method C recommended  
API specific guidances: Loteprednol, Dexamethasone / Tobramycin

# Potvin *et al.* (Method B)



# Potvin *et al.* (Method C)





# TSDs: Alternatives

- Methods by Potvin *et al.* (2008) limited to T/R of 0.95 and 80% power
  - Follow-up papers (T/R 0.95...0.90, 80...90% power)

reference	method	T/R	target power	CV	$\alpha_{adj.}$	max. $\alpha_{emp.}$
Potvin <i>et al.</i>	B	0.95	80%	10–100%	0.0294	0.0485
	C	0.95				0.0510
Montague <i>et al.</i>	D	0.90			0.0280	0.0518
Fuglsang	B	0.95	90%	10–80%	0.0284	0.0501
	D				0.0274	0.0503
	D	0.90			0.0269	0.0501

**Montague TH, Potvin D, DiLiberti CE, Hauck WW, Parr AF, and DJ Schuirmann**

*Additional results for 'Sequential design approaches for bioequivalence studies with crossover designs'*

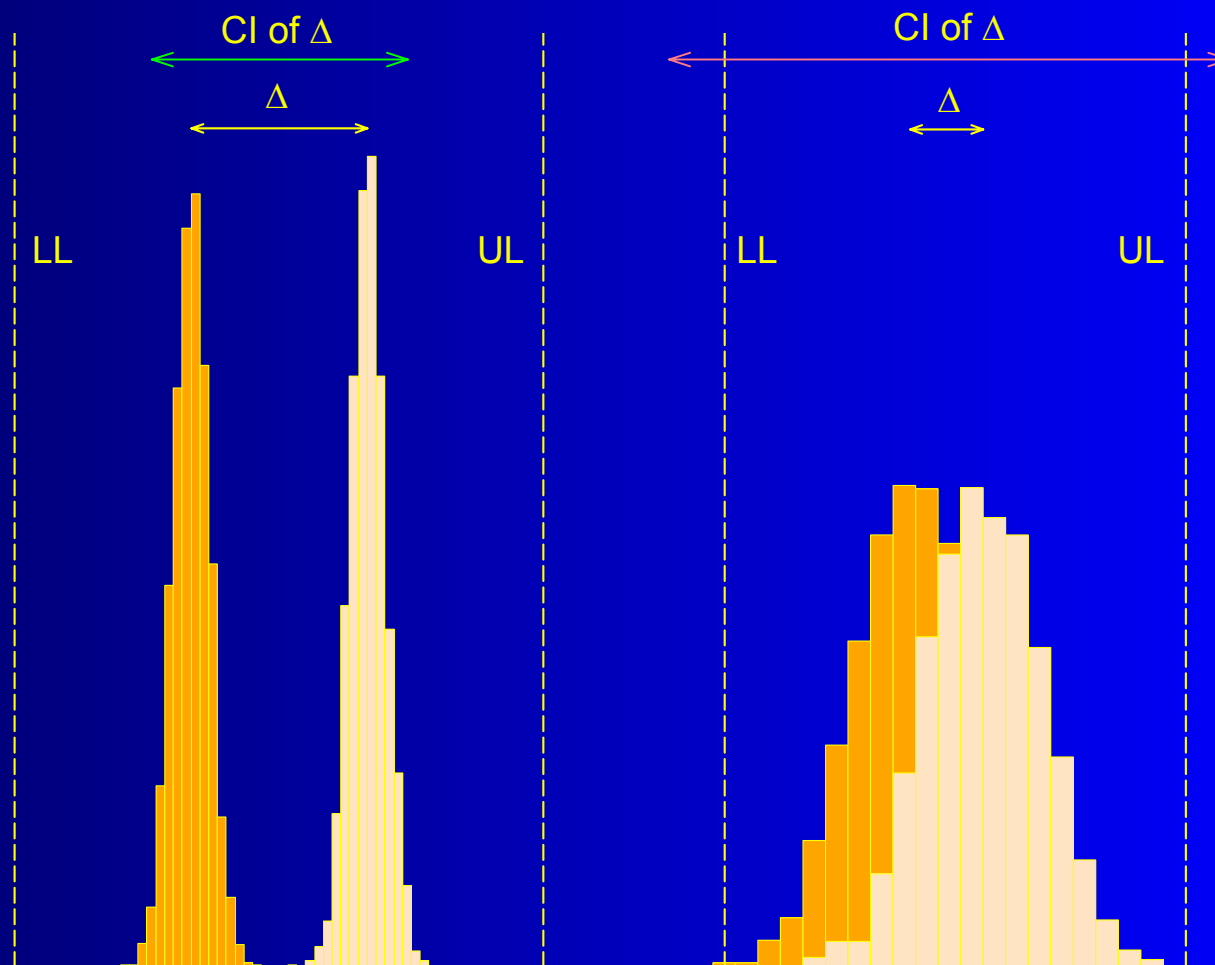
Pharmaceut Statist 11(1), 8–13 (2011) DOI: [10.1002/pst.483](https://doi.org/10.1002/pst.483)

**A Fuglsang**

*Sequential Bioequivalence Trial Designs with Increased Power and Controlled Type I Error Rates*

AAPS J 15(3), 659–61 (2013) DOI: [10.1208/s12248-013-9475-5](https://doi.org/10.1208/s12248-013-9475-5)

# High variability



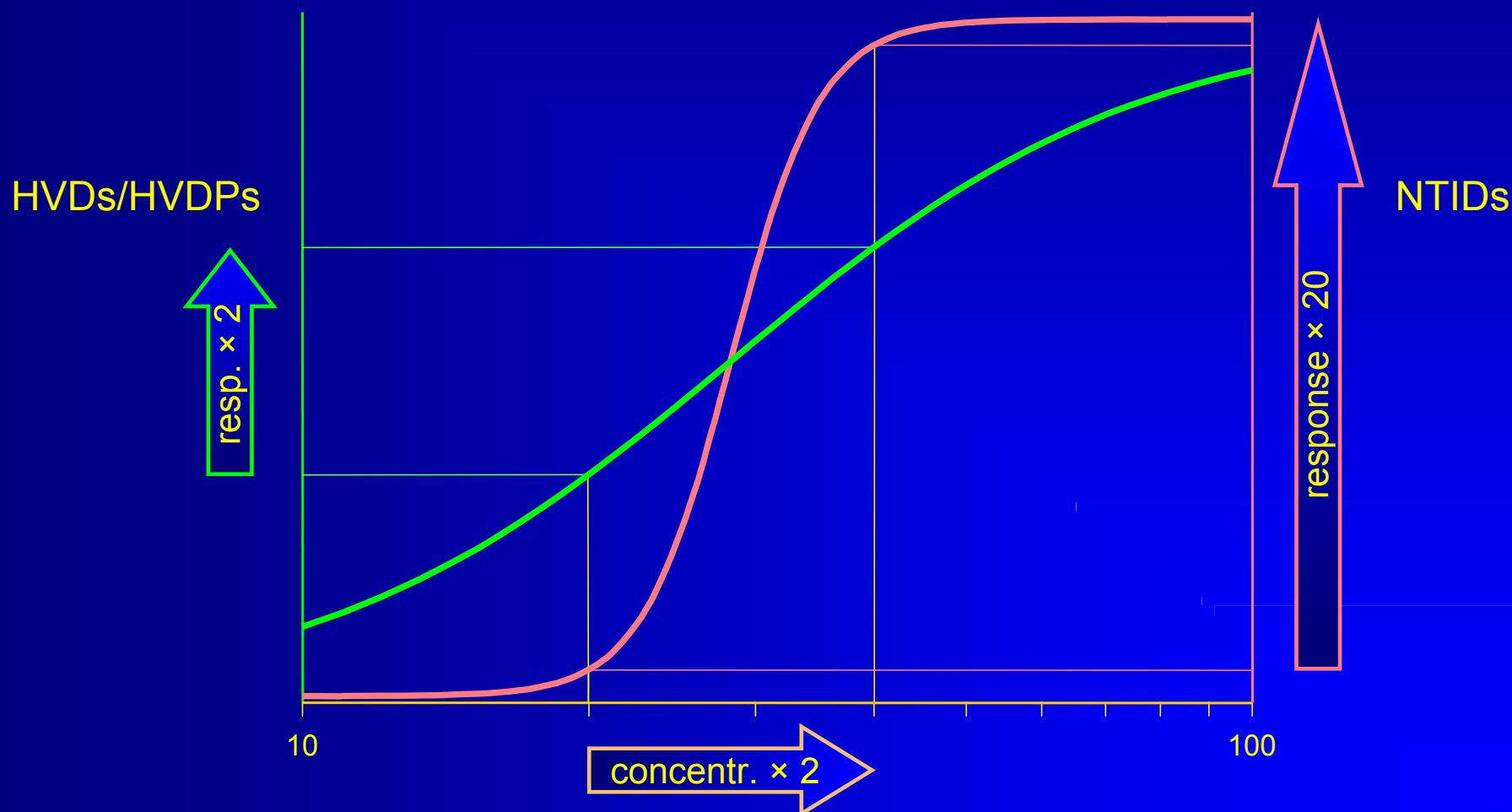
Modified from Fig. 1  
Tothfálusi *et al.* (2009)

Counterintuitive  
concept of BE:

Two formulations with  
a large difference in  
means are declared  
bioequivalent if vari-  
ances are low, but not  
bioequivalent – even  
if the difference is  
quite small – due to  
high variability.

# HVDs/HVDPs are safe

flat & steep PK/PD-curves



# High variability

- For Highly Variable Drugs / Drug Products (HVDs/HVDPs) it may be almost impossible to show BE with a reasonable sample size.
- The common 2×2 cross-over design over assumes Independent Identically Distributions (IID), which may not hold. If e.g., the variability of the reference is higher than the one of the test, one obtains a high common (pooled) variance and the test will be penalized for the 'bad' reference.

# Replicate designs

- Each subject is randomly assigned to sequences, where *at least one* of the treatments is administered *at least twice*
  - Not only the *global within-subject variability*, but also the *within-subject variability per treatment* may be estimated.
  - Smaller subject numbers compared to a standard  $2 \times 2 \times 2$  design – but outweighed by an increased number of periods. Note: Same overall number of individual treatments!

# Replicate designs

- Any replicate design can be evaluated according to 'classical' (unscaled) Average Bioequivalence (ABE)
- ABE mandatory if scaling not allowed
  - FDA:  $s_{WR} < 0.294$  ( $CV_{WR} < 30\%$ ); different models depend on design (e.g., SAS **Proc MIXED** for full replicate and SAS **Proc GLM** for partial replicate).
  - EMA:  $CV_{WR} \leq 30\%$ ; all fixed effects model according to 2011's Q&A-document preferred (e.g., SAS **Proc GLM**).
  - Even if scaling is not intended, replicate design give more informations about formulation(s)

# Application: HVDs/HVDPs

- $CV_{WR} > 30\%$

- ✓ USA Recommended in API specific guidances.  
Scaling for  $AUC$  and/or  $C_{max}$  acceptable,  
GMR 0.80 – 1.25;  $\geq 24$  subjects enrolled.

- ± EU Widening of acceptance range (only  $C_{max}$ ) to  
maximum of 69.84% – 143.19%),  
GMR 0.80 – 1.25.

- Demonstration that  $CV_{WR} > 30\%$  is not caused  
by outliers.

- Justification that the widened acceptance  
range is clinically irrelevant.



# Replicate designs

- Two-sequence three-period

T R T  
R T R

- Two-sequence four-period

T R T R  
R T R T

- and many others...

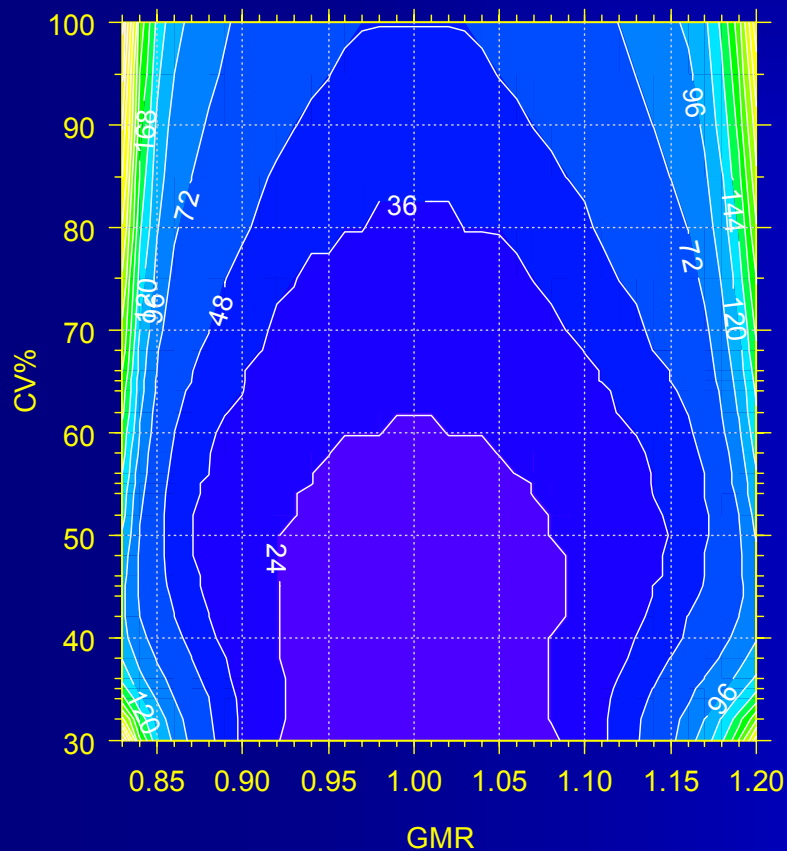
(FDA: TRR | RTR | RRT, aka 'partial replicate')

- The statistical model is complicated and depends on the actual design!

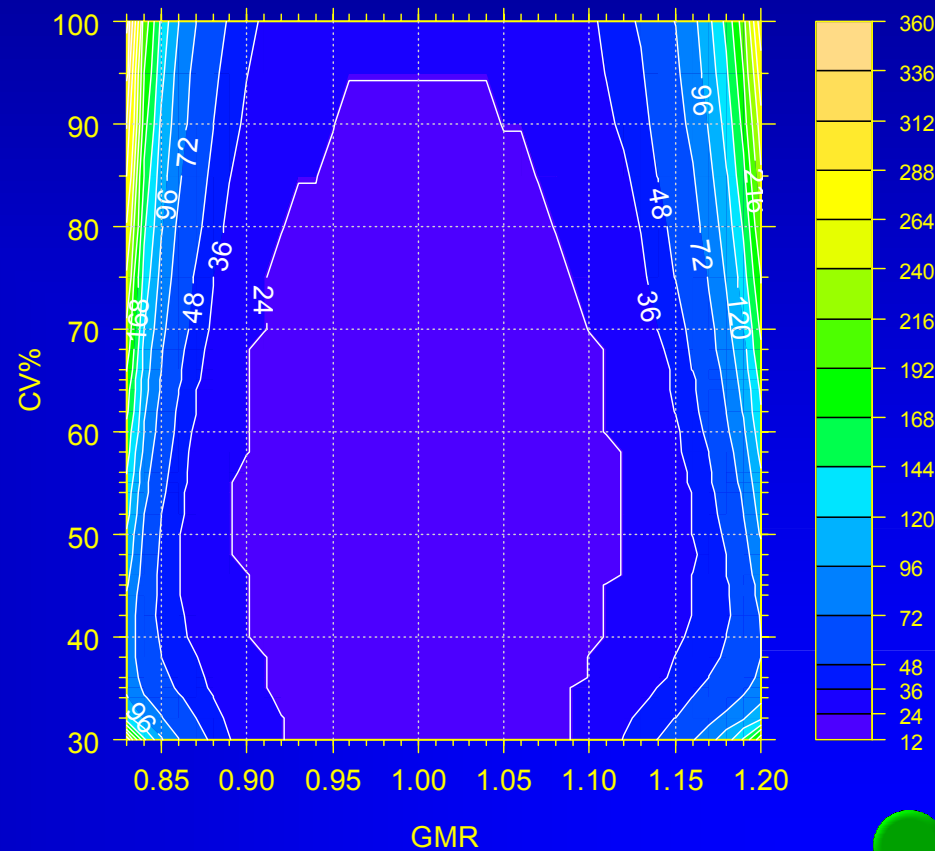
$$X_{ijkl} = \mu \cdot \pi_k \cdot \Phi_l \cdot s_{ij} \cdot e_{ijkl}$$

# HVDPs (EMA/FDA; sample sizes)

RTTR | TRTR, 80% power, EMA

sample  
size

RTTR | TRTR, 80% power, FDA

sample  
size

# HVDPs (EMA)

- EU GL on BE (2010)
  - Average Bioequivalence (ABE) with Expanding Limits (ABEL)
    - Based on  $\sigma_{WR}$  (the *intra*-subject standard deviation of the reference formulation) calculate the scaled acceptance range based on the regulatory constant  $k$  ( $\theta_s=0.760$ ); limited at  $CV_{WR}$  50%.

$$[L - U] = e^{\mp k \cdot \sigma_{WR}}$$

$CV_{WR}$	$L - U$
$\leq 30$	80.00 – 125.00
35	77.23 – 129.48
40	74.62 – 143.02
45	72.15 – 138.59
$\geq 50$	69.84 – 143.19

# HVDPs (EMA)

- Q&A document (March 2011)
  - Two methods proposed (Method A preferred)
    - **Method A:** All effects fixed; assumes equal variances of test and reference, and no subject-by-formulation interaction; only a common within (*intra-*) subject variance is estimated.
    - **Method B:** Similar to A, but random effects for subjects. Common within (*intra-*) subject variance and between (*inter-*) subject variance are estimated.
  - Outliers: Boxplots (of model residuals?) suggested.

*Questions & Answers on the Revised EMA Bioequivalence Guideline  
Summary of the discussions held at the 3<sup>rd</sup> EGA Symposium on Bioequivalence  
June 2010, London  
[http://www.egagenerics.com/doc/EGA\\_BEQ\\_Q&A\\_WEB\\_QA\\_1\\_32.pdf](http://www.egagenerics.com/doc/EGA_BEQ_Q&A_WEB_QA_1_32.pdf)*

# Example datasets (EMA)

- Q&A document (March 2011)
  - Data set I  
RTRT | TRTR full replicate, 77 subjects, imbalanced, incomplete
    - FDA
      - $s_{WR} 0.446 \geq 0.294 \rightarrow$  apply RSABE ( $CV_{WR} 46.96\%$ )
        - a. critbound  $-0.0921 \leq 0$  and
        - b. PE  $115.46\% \subset 80.00-125.00\%$  ✓
    - EMA
      - $CV_{WR} 46.96\% \rightarrow$  apply ABEL ( $> 30\%$ )
      - Scaled Acceptance Range: 71.23–140.40%
      - Method A: 90% CI 107.11–124.89%  $\subset$  AR; PE 115.66% ✓
      - Method B: 90% CI 107.17–124.97%  $\subset$  AR; PE 115.73% ✓

# Example datasets (EMA)

- Q&A document (March 2011)

- Data set II

TRR | RTR | RRT partial replicate, 24 subjects, balanced, complete

- FDA

$s_{WR}$  0.114 < 0.294 → apply ABE ( $CV_{WR}$  11.43%)  
90% CI 97.05–107.76  $\subset$  AR ( $CV_{intra}$  11.55%) ✓

- EMA

- $CV_{WR}$  11.17% → apply ABE ( $\leq 30\%$ )
      - Method A: 90% CI 97.32–107.46%  $\subset$  AR; PE 102.26% ✓
      - Method B: 90% CI 97.32–107.46%  $\subset$  AR; PE 102.26% ✓
      - A/B:  $CV_{intra}$  11.86%

# Outliers (EMA)

- EMA GL on BE (2010), Section 4.1.10
  - The applicant should justify that the calculated intra-subject variability is a reliable estimate and that it is not the result of outliers.
- EGA/EMA Q&A (2010)
  - Question:  
How should a company proceed if outlier values are observed for the reference product in a replicate design study for a Highly Variable Drug Product (HVDP)?





# Outliers (EMA)

- EGA/EMA Q&A (2010)

- Answer:

The outlier cannot be removed from evaluation [...] but should not be taken into account for calculation of within-subject variability and extension of the acceptance range.

An outlier test is not an expectation of the medicines agencies but outliers could be shown by a box plot. This would allow the medicines agencies to compare the data between them.



# Outliers (EMA)

- Data set I (full replicate)

- $CV_{WR}$  46.96%

- EL 71.23–140.40%

- Method A: 107.11–124.89%

- Method B: 107.17–124.97%

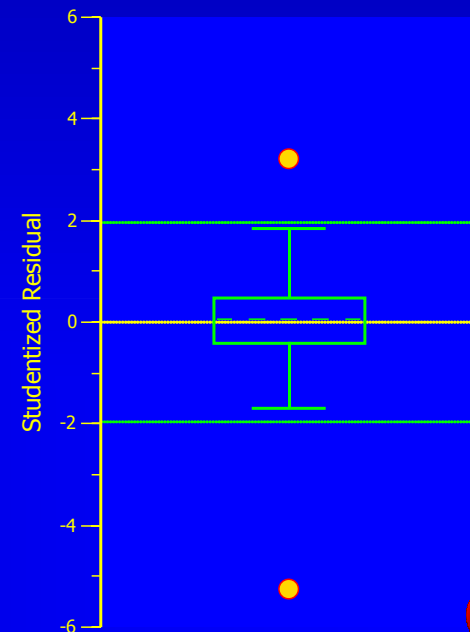
- But there *are* two outliers!

- By excluding subjects 45 and 52

- $CV_{WR}$  drops to 32.16%.

- EL 78.79–126.93%

- Almost no more gain compared to conventional limits...



شكرا لك!

# Pharmacokinetic and Statistical Analysis of BE Data

## *Open Questions?*



Helmut Schütz  
**BEBAC**

Consultancy Services for  
Bioequivalence and Bioavailability Studies  
1070 Vienna, Austria  
[helmut.schuetz@bebac.at](mailto:helmut.schuetz@bebac.at)

# To bear in Remembrance...

To call the statistician after the experiment is done may be no more than asking him to perform a *post-mortem* examination: he may be able to say what the experiment died of.

*Ronald A. Fisher*



[The] impatience with ambiguity can be criticized in the phrase:

*absence of evidence is not evidence of absence.*

*Carl Sagan*

[...] our greatest mistake would be to forget that data is used for serious decisions in the very real world, and bad information causes suffering and death.

*Ben Goldacre*

