

Inflation of the Type I Error in Reference-scaled Average Bioequivalence

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Study Designs

The more 'sophisticated' a design is,
the more information can be extracted.

Information

- Hierarchy of designs:

Full replicate (RTRT | TRTR or RTR | TRT) ↗

Partial replicate (RRT | RTR | TRR) ↗

2×2×2 crossover (RT | TR) ↗

Parallel (R | T)

- Variances which can be estimated:

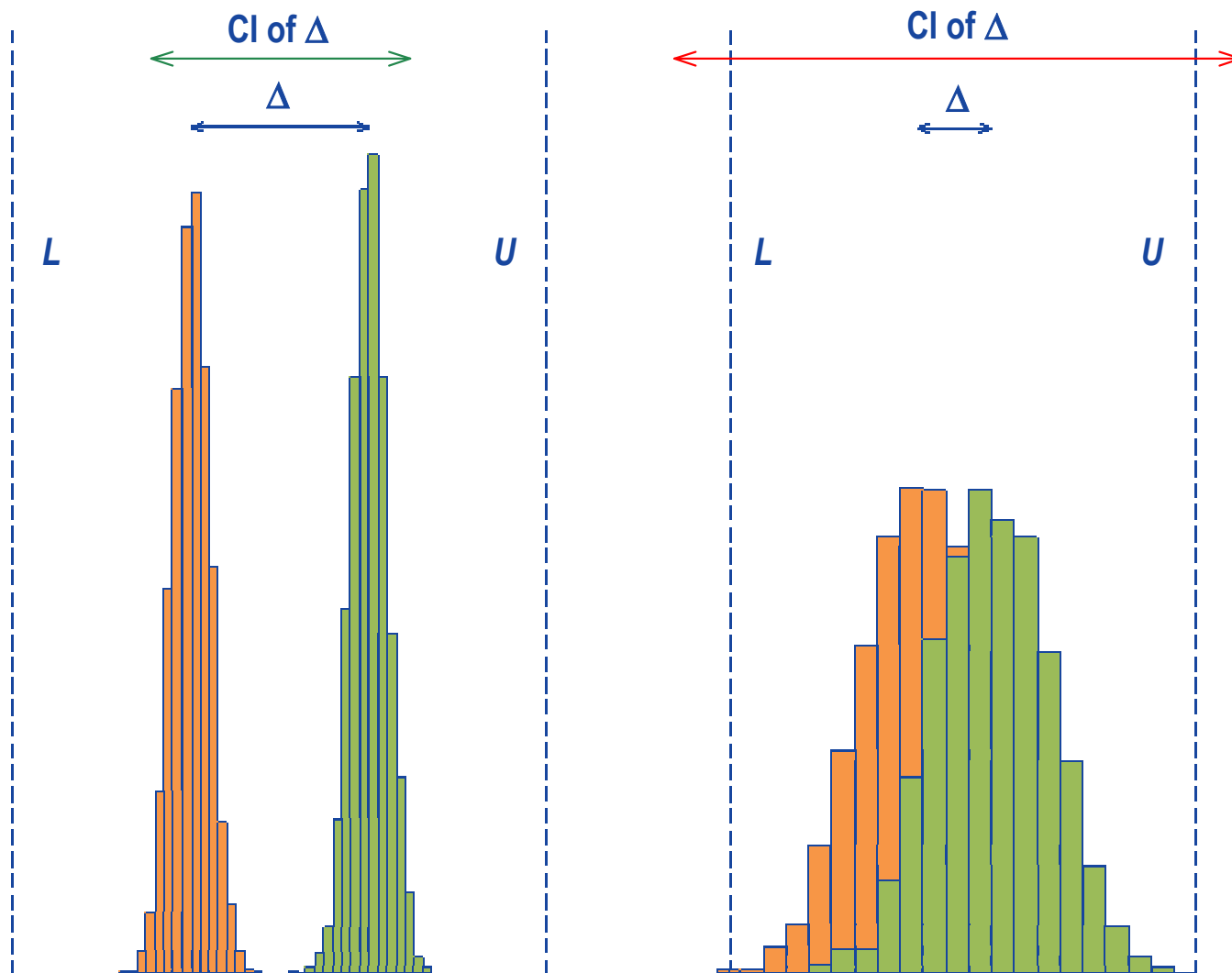
Parallel: total variance (*pooled* of between + within subjects)

2×2×2 crossover: + *between, within* subjects ↗

Partial replicate: + within subjects (*of R*) ↗

Full replicate: + within subjects (*of R and T*) ↗

Highly Variable Drugs / Drug Products



Counterintuitive concept of BE:

Two formulations with a large difference in means are declared bioequivalent if variances are low, but not BE – even if the difference is quite small – due to high variability.

Modified from Tothfaluasi *et al.* (2009), Fig. 1

HVD(P)s – Reference-scaling

It may be almost impossible to demonstrate BE with a reasonable sample size.

- Reference-scaling (*i.e.*, widening the acceptance range based of the variability of the reference) in 2010 introduced by the FDA and EMA and in 2016 by Health Canada.
 - Requires a replicate design, where at least the reference product is administered twice.
 - Smaller sample sizes compared to a standard 2×2×2 design but outweighed by increased number of periods.
 - Similar total number of individual treatments.
 - Any replicate design can be evaluated for ‘classical’ (unscaled) Average Bioequivalence (ABE) as well. Switching CV_{wR} 30%:
 - FDA: AUC and C_{max}
 - EMA: C_{max} ; MR products additionally: $C_{ss,min}$, $C_{ss,T}$, partial $AUCs$
 - Health Canada: AUC

HVD(P)s – Reference-scaling

Models (in log-scale).

- **ABE Model:**

- A difference Δ of $\leq 20\%$ is considered to be clinically not relevant.
- The limits $[L, U]$ of the acceptance range are fixed to $\log(1 - \Delta) = \log((1 - \Delta)^{-1})$ or $L \sim -0.2231$ and $U \sim +0.2231$.
- The consumer risk is fixed with 0.05. BE is concluded if the $100(1 - 2\alpha)$ confidence interval lies entirely within the acceptance range.

$$-\theta_A \leq \mu_T - \mu_R \leq +\theta_A$$

- **SABEL Model:**

- Switching condition θ_S is derived from the regulatory standardized variation σ_0 (proportionality between acceptance limits in log-scale and σ_{wR} in the highly variable region).

$$-\theta_S \leq \frac{\mu_T - \mu_R}{\sigma_{wR}} \leq +\theta_S$$

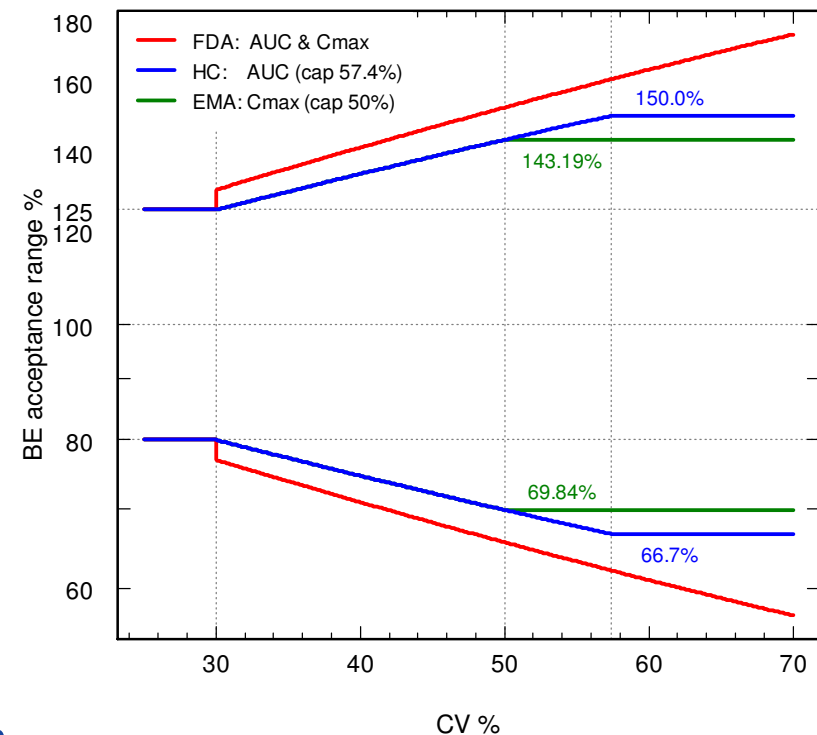
HVD(P)s – Reference-scaling

Regulatory Approaches.

- Bioequivalence limits derived from σ_0 and σ_{wR}

$$\theta_s = \frac{\log(1.25)}{\sigma_0}, \quad [L, U] = e^{\pm\theta_s \cdot \sigma_{wR}}$$

- **FDA**
 - Scaling σ_{wR} 0.25 (θ_s 0.893) but applicable at $CV_{wR} \geq 30\%$.
 - Discontinuity at CV_{wR} 30%.
- **EMA**
 - Scaling σ_0 0.2936 (θ_s 0.760).
 - Upper cap at CV_{wR} 50%.
- **Health Canada**
 - Like EMA but upper cap at CV_{wR} 57.4%.



HVD(P)s – Reference-scaling

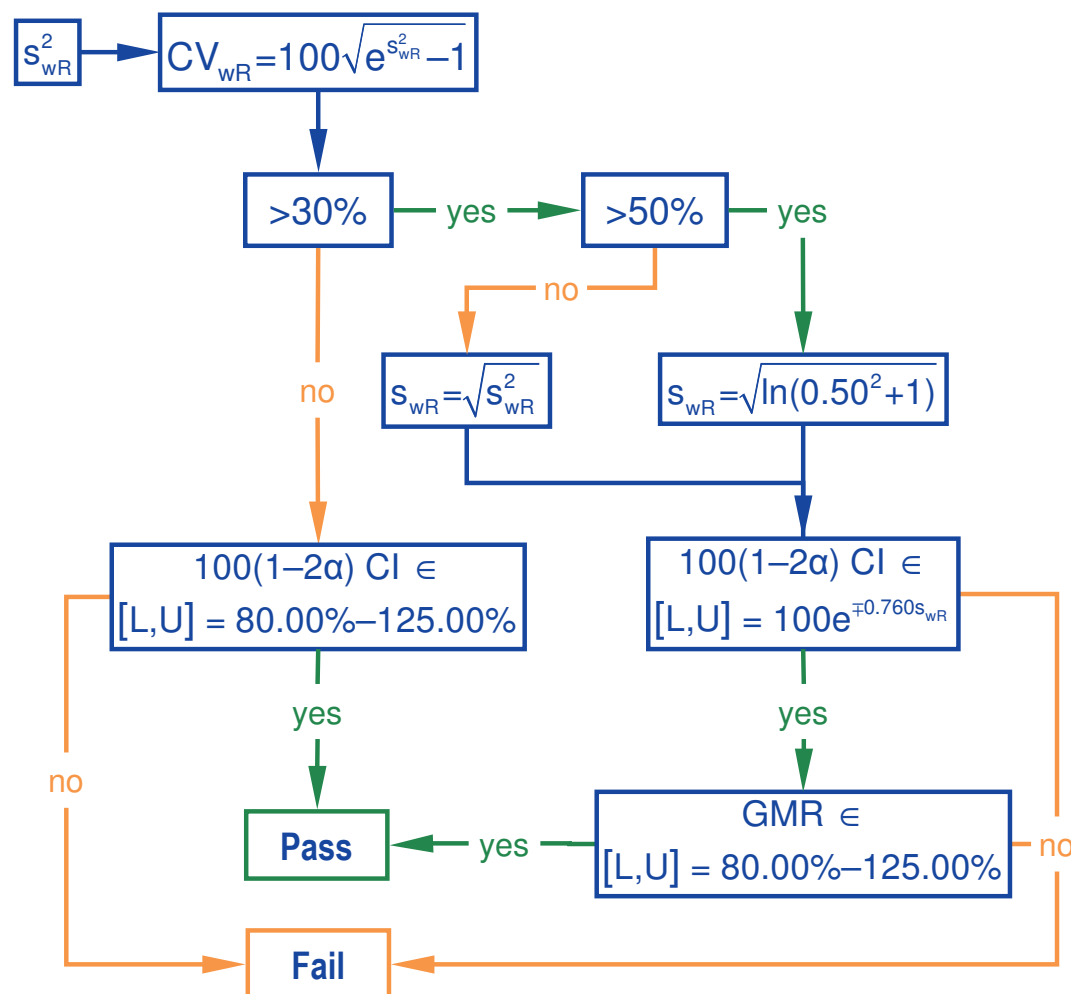
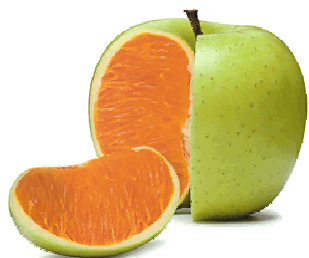
The EMA's Approach.

- Average Bioequivalence with Expanding Limits – ABEL (crippled from Endrényi and Tóthfalusi 2009).
 - Justification that the widened acceptance range is clinically not relevant (important – different to the FDA).
 - Assumes identical variances of T and R [*sic*] like in a 2×2×2.
 - All fixed effects model according to the Q&A-document preferred.
 - Mixed-effects model (allowing for unequal variances) is 'not compatible with CHMP guideline'...
 - Scaling limited at a maximum of CV_{wR} 50% (*i.e.*, to 69.84 – 143.19%).
 - *GMR* within 0.8000 – 1.2500.
 - Demonstration that $CV_{wR} > 30\%$ is not caused by outliers (box plots of studentized intra-subject residuals?)...
 - ≥ 12 subjects in sequence RTR of the 3-period full replicate design.

HVD(P)s – Reference-scaling

The EMA's Approach.

- **Decision Scheme.**
 - The Null Hypothesis is *specified* in the face of the data.
 - Acceptance limits themselves become random variables.
 - Type I Error (consumer risk) might be inflated.



HVD(P)s – Reference-scaling

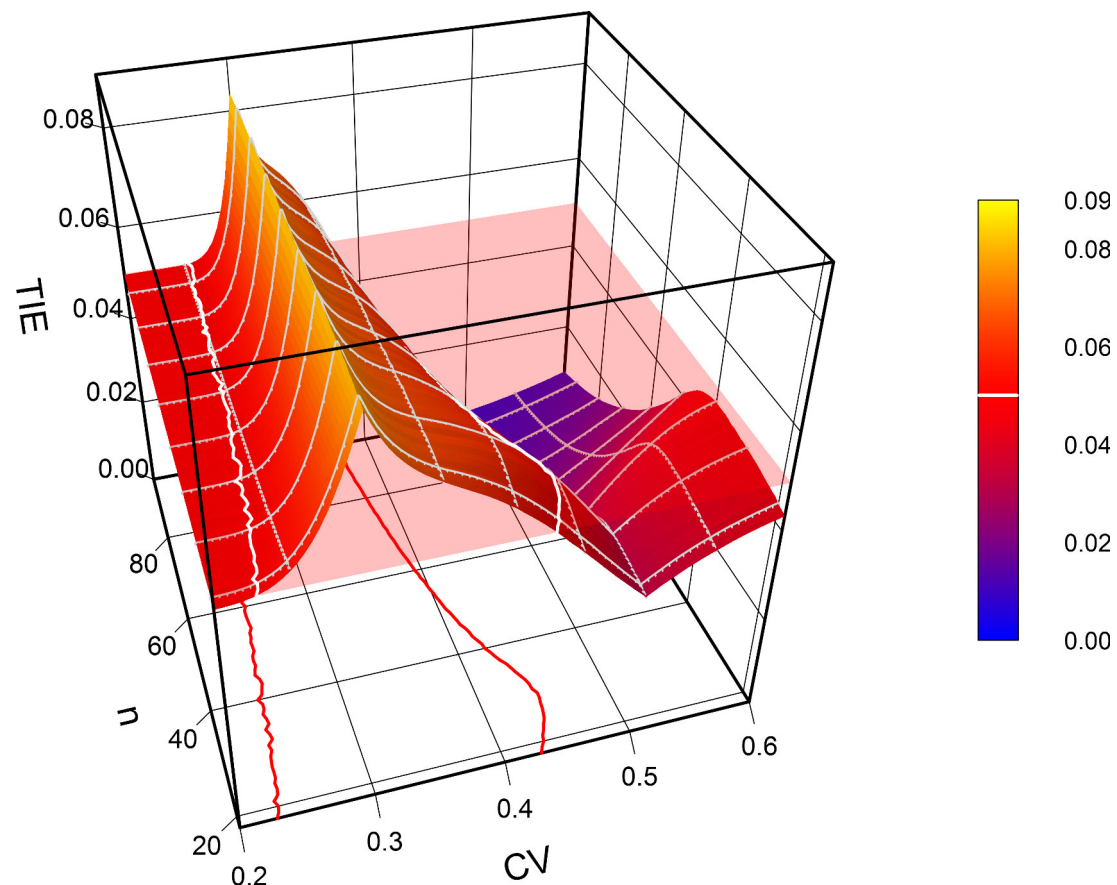
Assessing the Type I Error (TIE).

- TIE = falsely concluding BE at the limits of the acceptance range.
- Due to the decision scheme direct calculation of the TIE at the scaled limits is not possible;
 - extensive simulations required (10^6 BE studies mandatory).
- Inflation of the TIE suspected.
(Chow *et al.* 2002, Willavazie/Morgenthien 2006, Chow/Liu 2009, Patterson/Jones 2012).
- Confirmed.
 - EMA's ABEL
(Tóthfalusi/Endrényi 2009, BEBA-Forum 2013, Wonnemann *et al.* 2015, Muñoz *et al.* 2016, Labes/Schütz 2016).
 - FDA's RSABE
(Tóthfalusi/Endrényi 2009, BEBA-Forum 2013, Muñoz *et al.* 2016).

HVD(P)s – Reference-scaling

Example for ABEL

- RTRT | TRTR
sample size 18 – 96
 CV_{wR} 20% – 60%
 - TIE_{max} 0.0837.
 - Relative increase of the consumer risk 67%!



HVD(P)s – Reference-scaling

What is going on here?

- SABC is stated in model *parameters* ...

$$-\theta_S \leq \frac{\mu_T - \mu_R}{\sigma_{wR}} \leq +\theta_S$$

... which are *unknown*.

- Only their *estimates* (GMR, s_{wR}) are accessible in the actual study.
- At CV_{wR} 30% the decision to scale will be wrong in ~50% of cases.
- If moving away from 30% the chances of a wrong decision decrease and hence, the TIE.
- At high CVs (>43%) both the scaling cap and the *GMR*-restriction help to maintain the TIE <0.05).

HVD(P)s – Reference-scaling

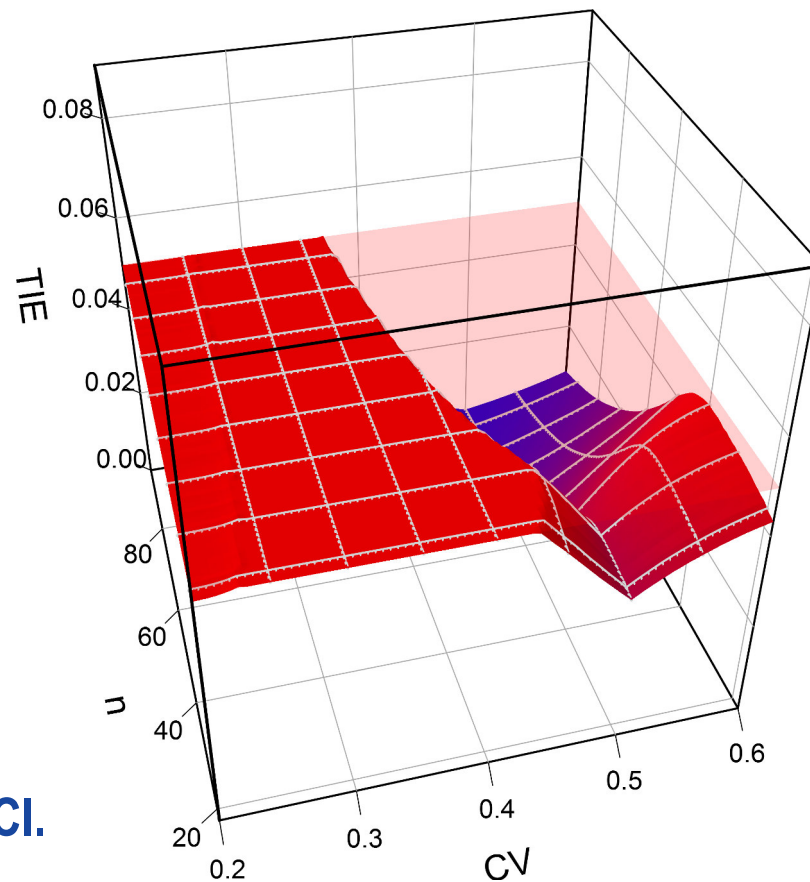
Outlook.

- Utopia
 - Agencies collect CV_{wR} from submitted studies. Pool them, adjust for designs / degrees of freedom. The EMA publishes a fixed acceptance range in the product-specific guidance. No need for replicate studies any more. $2 \times 2 \times 2$ crossovers evaluated by ABE would be sufficient.
- Halfbaked
 - Hope [*sic*] that e.g., Bonferroni preserves the consumer risk. Still apply ABEL, but with a 95% CI ($\alpha 0.025$).
 - Drawback: Loss of power, substantial increase in sample sizes.
- Proposal
 - Iteratively adjust α based on the study's CV_{wR} and sample size – in such a way that the consumer risk is preserved (Labes/Schütz 2016).

ABEL (iteratively adjusted α)

Previous example

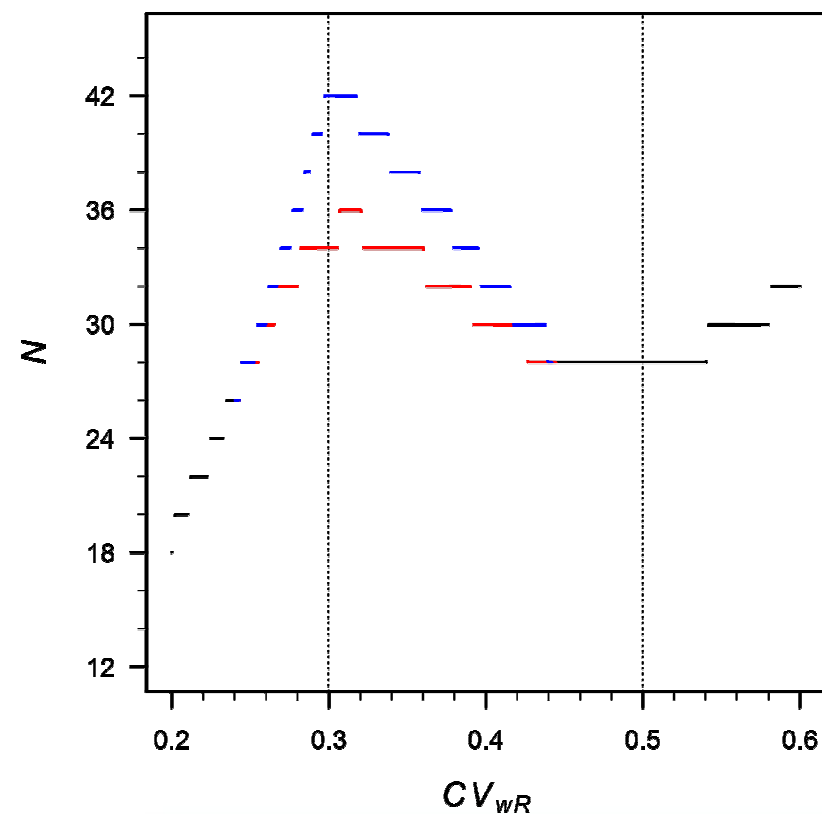
- Algorithm
 - Assess the TIE for the nominal α 0.05.
 - If the TIE ≤ 0.05 , stop.
 - Otherwise adjust α (downwards) until the TIE = 0.05.
 - At CV_{WR} 30% (dependent on the sample size) α_{adj} is 0.0273 – 0.0300;
 → use a 94.00 – 94.54% CI.



ABEL (iteratively adjusted α)

Potential impact on the sample size.

- Example: RTRT | TRTR, θ_0 0.90, target power 0.80.
 - Moderate in the critical region (— —).
 - CV_{WR} 30%: **36** → **42** (+17%);
 - CV_{WR} 35%: **34** → **38** (+12%);
 - CV_{WR} 40%: **30** → **32** (+7%).
 - None outside (—).



ABEL (iteratively adjusted α)

Example (RTRT | TRTR, expected CV_{WR} 35%, θ_0 0.90, target power 0.80); R package PowerTOST ($\geq 1.3-3$).

- Estimate the sample size.

```
sampleN.scABEL(CV=0.35, theta0=0.90, targetpower=0.80, design="2x2x4",
               details=FALSE, print=FALSE)[["Sample size"]]
[1] 34
```

- Estimate the empiric TIE for this study.

```
UL <- scABEL(CV=0.35)[["upper"]] # scaled limit (1.2948 for CVwr 0.35)
power.scABEL(CV=0.35, theta0=UL, n=34, design="2x2x4", nsims=1e6)
[1] 0.065566
```

- Iteratively adjust α .

```
scABEL.ad(CV=0.35, n=34, design="2x2x4")
+++++++ scaled (widened) ABEL ++++++
iteratively adjusted alpha
-----
CVWR 0.35, n(i) 17|17 (N 34)
Nominal alpha           : 0.05
Null (true) ratio       : 0.9000
Regulatory settings     : EMA (ABEL)
Empiric TIE for alpha 0.0500 : 0.06557
Power for theta0 0.900  : 0.812
Iteratively adjusted alpha : 0.03630
Empiric TIE for adjusted alpha: 0.05000
Power for theta0 0.900  : 0.773
```

ABEL (iteratively adjusted α)

- Optionally compensate for the loss in power (0.812 \rightarrow 0.773) by increasing the sample size:

```
sampleN.scABEL.ad(CV=0.35, theta0=0.90, targetpower=0.80, design="2x2x4")
+++++++ scaled (widened) ABEL ++++++
          Sample size estimation
          for iteratively adjusted alpha
```

```
-----
Study design: 2x2x4 (RTRT|TRTR)
Expected CVWR 0.35
Nominal alpha      : 0.05
Null (true) ratio  : 0.9000
Target power       : 0.8
Regulatory settings: EMA (ABEL)
Switching CVWR     : 30%
Regulatory constant: 0.760
Expanded limits    : 0.7723...1.2948
Upper scaling cap  : CVWR 0.5
PE constraints     : 0.8000...1.2500
n 38, adj. alpha: 0.03610 (power 0.8100), TIE: 0.05000
```

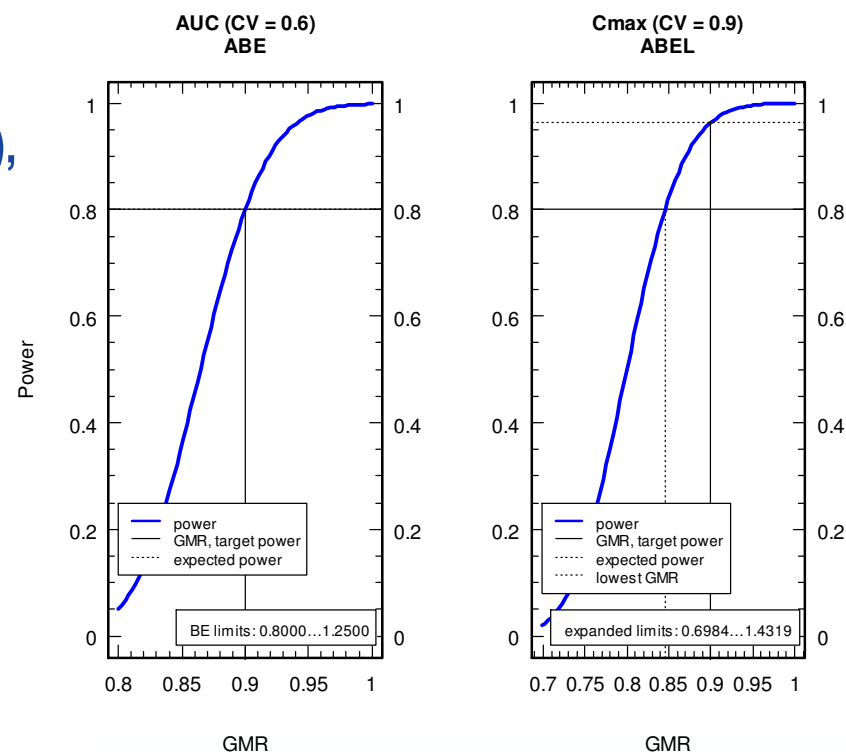
— n 34 \rightarrow 38 (+12%), power 0.773 \rightarrow 0.810, α_{adj} 0.0363 \rightarrow 0.0361.

Side Effect

Allowing ABEL only for C_{max}

- Some drugs show high variability in AUC as well.
 - Since in such a case the sample size will be mandated by AUC , products with high deviations in C_{max} will be approved.
 - Example: CV_{wR} 90% (C_{max}), 60% (AUC), θ_0 0.90, target power 80% → the study is ‘overpowered’ for C_{max} ; C_{max} -GMRs of [0.846–1.183] will pass BE. Really desirable?
 - With the FDA’s RSABE the study could be performed in only 34 subjects...

ABEL (EMA): design RTRT|TRTR, target power = 0.8, n = 138 (sample size dependent on AUC)



Inflation of the Type I Error in Reference-scaled Average Bioequivalence

Thank You!
Open Questions?



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To bear in Remembrance...

The fundamental cause of trouble in the world today is that the stupid are cocksure while the intelligent are full of doubt.

Bertrand Russell



100% of all disasters are failures of design, not analysis.

Ronald G. Marks

My definition of an expert in any field is a person who knows enough about what's really going on to be scared.

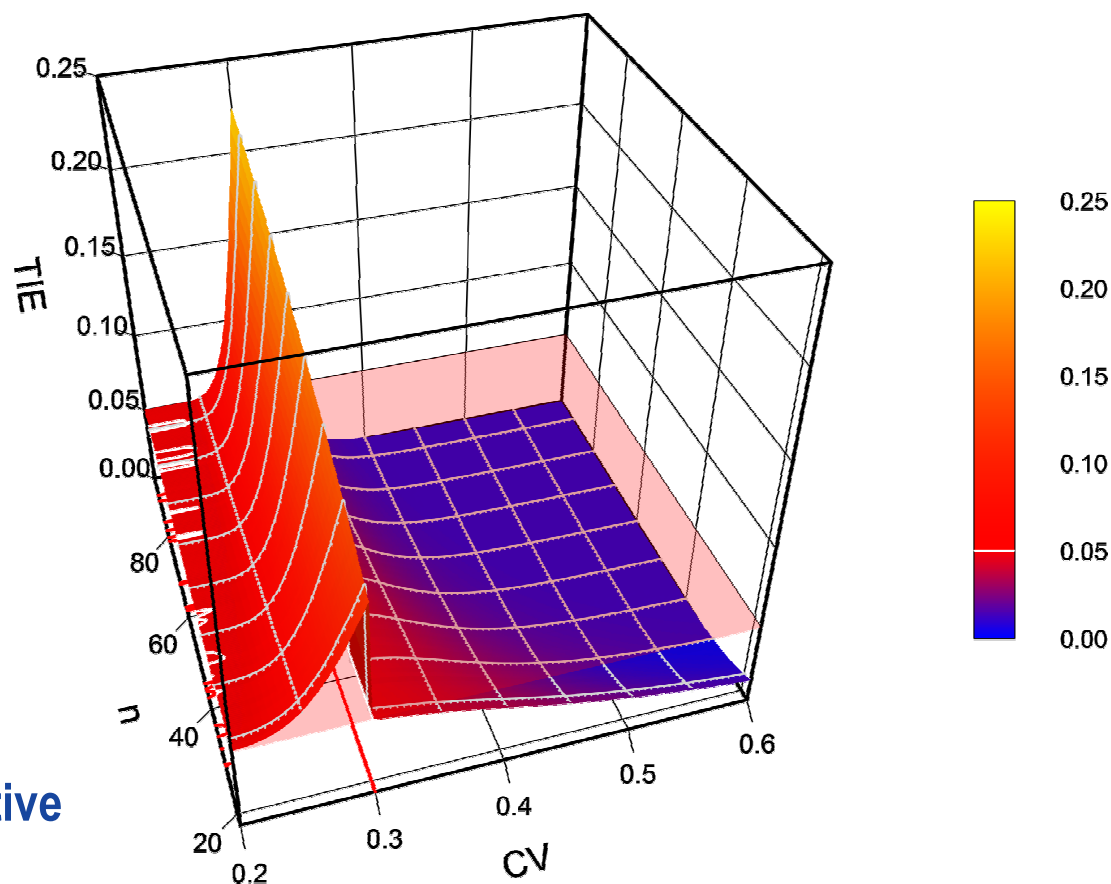
Phillip J. Plauger



Backup

Example for the FDA's RSABE

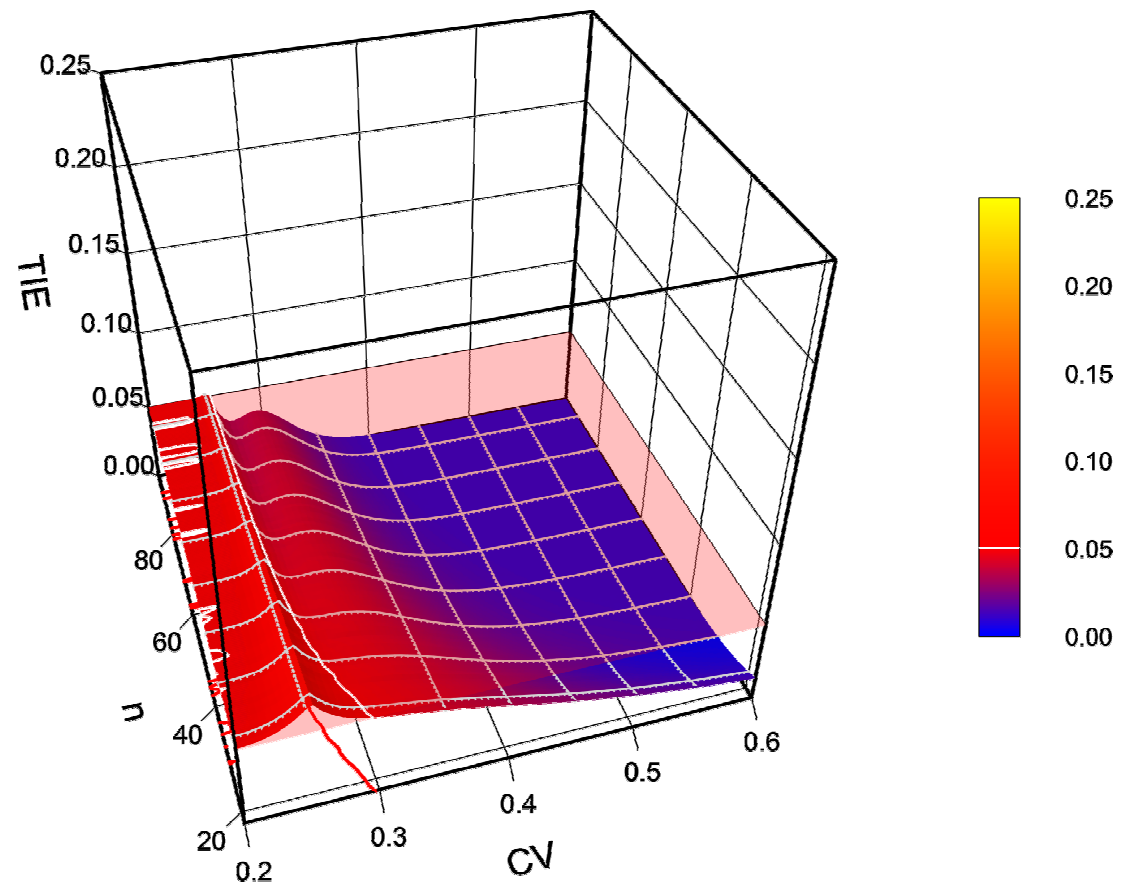
- RTRT | TRTR
sample size 18 – 96
 CV_{wR} 20% – 60%
 - TIE_{max} 0.2245.
 - Relative increase of the consumer risk 349%!
 - TIE more dependent on the sample size than in ABEL.
 - However, no inflation of the TIE for $CV_{wR} > 30\%$; RSABE is very conservative for 'true' HVD(P)s.



Backup

FDA's desired consumer risk model (Davit *et al.* 2012)

- Previous example
 - TIE assessed not at the scaled limits but
 - at 1.25 if $CV_{WR} \leq 25.4\%$ or
 - at $e^{0.893 \cdot \sigma_{WR}}$ otherwise.
 - TIE_{max} 0.0668.
 - László Endrényi: “Hocus pocus!”



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