

# Establishing the Biostudy Statistical Design

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# Study Designs

The more 'sophisticated' a design is,  
the more information can be extracted.

Information

- Hierarchy of designs:

Full replicate (RTRT | TRTR or RTR | TRT) ↗

Partial replicate (RRT | RTR | TRR) ↗

2×2×2 cross-over (RT | TR) ↗

Parallel (R | T)

- Variances which can be estimated:

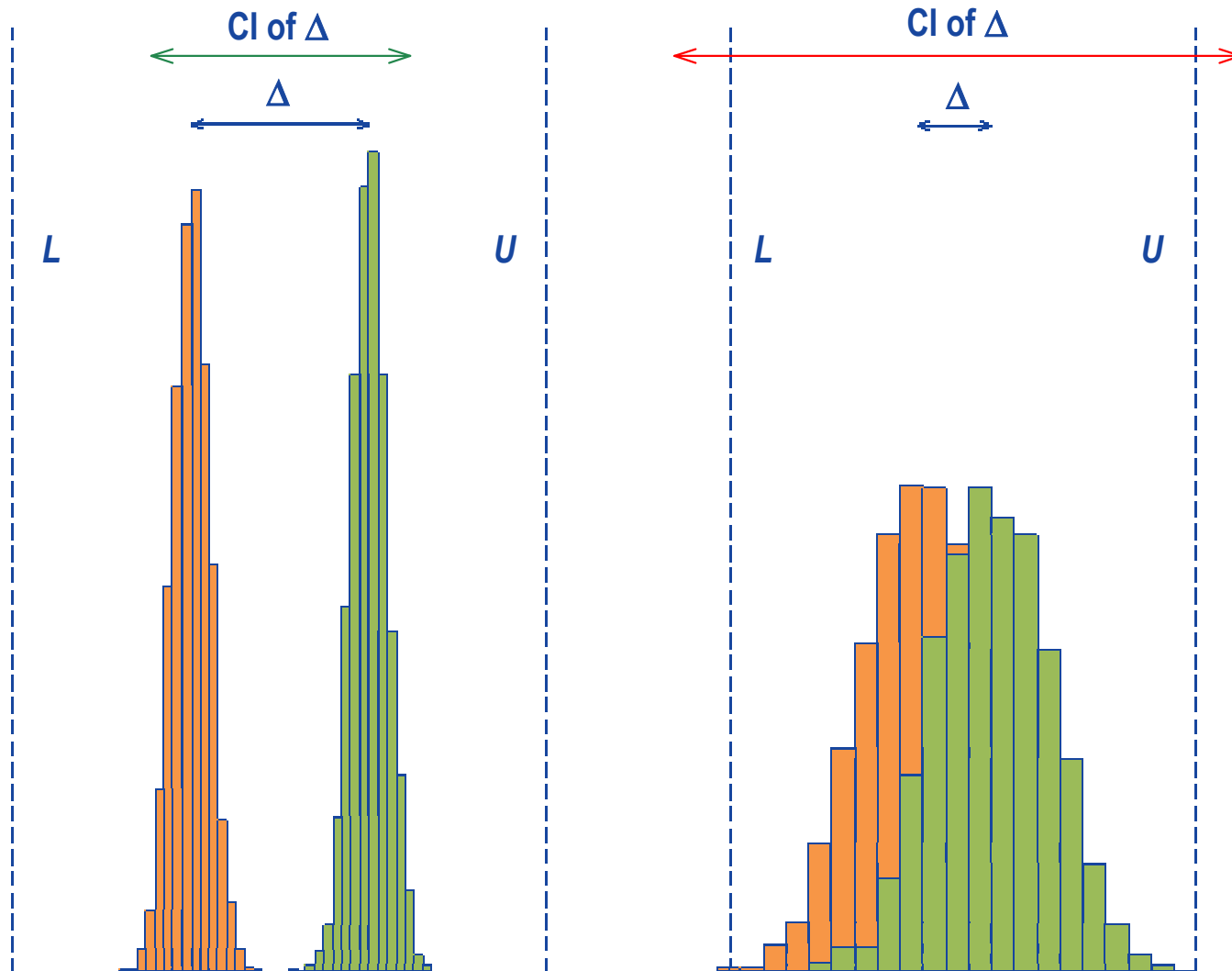
Parallel: *total variance (pooled of between + within subjects)*

2×2×2 cross-over: + *between, within subjects* ↗

Partial replicate: + *within subjects (of R)* ↗

Full replicate: + *within subjects (of R and T)* ↗

# Highly Variable Drugs / Drug Products



**Counterintuitive concept of BE:**

Two formulations with a large difference in means are declared bioequivalent if variances are low, but not BE – even if the difference is quite small – due to high variability.

Modified from Tothfaluasi *et al.* (2009), Fig. 1

# HVD(P)s – Reference-scaling

It may be almost impossible to demonstrate ABE with a reasonable sample size.

- Reference-scaling (*i.e.*, widening the acceptance range based of the variability of the reference) in 2010 introduced by the FDA and EMA and in 2016 by Health Canada.
  - Requires a replicate design, where at least the reference product is administered twice.
  - Smaller sample sizes compared to a standard 2×2×2 design but outweighed by increased number of periods.
  - Similar total number of individual treatments.
  - Any replicate design can be evaluated for ‘classical’ (unscaled) Average Bioequivalence (ABE) as well. Switching  $CV_{wR}$  30%:
    - FDA:  $AUC$  and  $C_{max}$
    - EMA:  $C_{max}$ ; MR products additionally:  $C_{ss,T}$ ,  $C_{ss,T}$ , partial  $AUCs$
    - Health Canada:  $AUC$

# HVD(P)s – Reference-scaling

## Models (in log-scale).

- **ABE Model:**

- A difference  $\Delta$  of  $\leq 20\%$  is considered to be clinically not relevant.
- The limits  $[L, U]$  of the acceptance range are fixed to  $\log(1 - \Delta) = \log((1 - \Delta)^{-1})$  or  $L \sim -0.2231$  and  $U \sim +0.2231$ .
- The consumer risk ( $\alpha$ ) is fixed with 0.05. BE is concluded if the  $100(1 - 2\alpha)$  confidence interval lies entirely within the acceptance range.

$$-\theta_A \leq \mu_T - \mu_R \leq +\theta_A$$

- **SABEL Model:**

- Switching condition  $\theta_S$  is derived from the regulatory standardized variation  $\sigma_0$  (proportionality between acceptance limits in log-scale and  $\sigma_{wR}$  in the highly variable region).

$$-\theta_S \leq \frac{\mu_T - \mu_R}{\sigma_{wR}} \leq +\theta_S$$

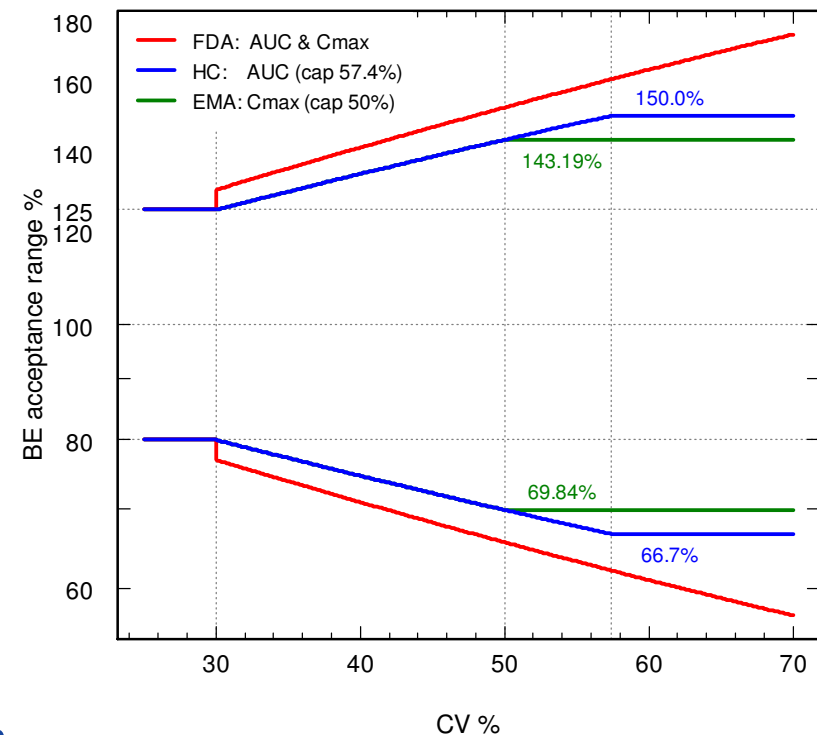
# HVD(P)s – Reference-scaling

## Regulatory Approaches.

- Bioequivalence limits derived from  $\sigma_0$  and  $\sigma_{wR}$

$$\theta_s = \frac{\log(1.25)}{\sigma_0}, \quad [L, U] = e^{\pm\theta_s \cdot \sigma_{wR}}$$

- **FDA**
  - Scaling  $\sigma_{wR}$  0.25 ( $\theta_s$  0.893) but applicable at  $CV_{wR} \geq 30\%$ .
  - Discontinuity at  $CV_{wR}$  30%.
- **EMA**
  - Scaling  $\sigma_0$  0.2936 ( $\theta_s$  0.760).
  - Upper cap at  $CV_{wR}$  50%.
- **Health Canada**
  - Like EMA but upper cap at  $CV_{wR}$  57.4%.



# HVD(P)s – Reference-scaling

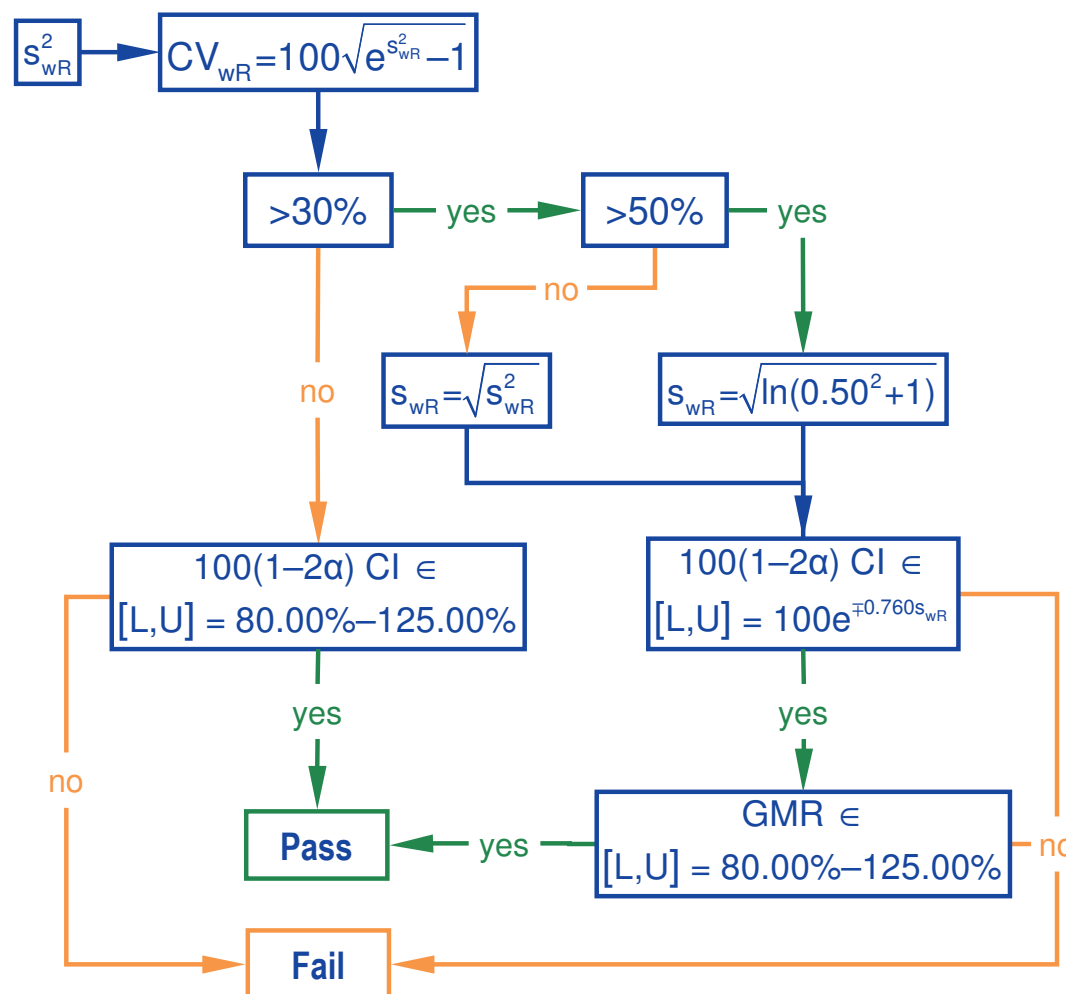
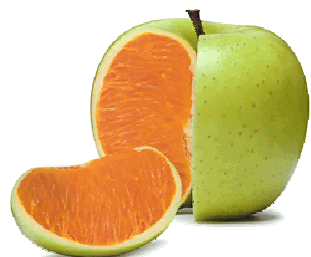
## The EMA's Approach.

- Average Bioequivalence with Expanding Limits – ABEL (crippled from Endrényi and Tóthfalusi 2009).
  - Justification that the widened acceptance range is clinically not relevant (important – different to the FDA).
  - Assumes identical variances of  $T$  and  $R$  [sic] like in a  $2 \times 2 \times 2$ .
  - All fixed effects model according to the Q&A-document preferred.
  - Mixed-effects model (allowing for unequal variances) is 'not compatible with CHMP guideline'...
  - Scaling limited at a maximum of  $CV_{WR}$  50% (i.e., to 69.84 – 143.19%).
  - $GMR$  within 0.8000 – 1.2500.
  - Demonstration that  $CV_{WR} > 30\%$  is not caused by outliers (box plots of studentized intra-subject residuals?)...
  - $\geq 12$  subjects in sequence RTR of the 3-period full replicate design.

# HVD(P)s – Reference-scaling

## The EMA's Approach.

- **Decision Scheme.**
  - The Null Hypothesis is *specified* in the face of the data.
  - Acceptance limits themselves become random variables.
  - Type I Error (consumer risk) might be inflated.





# HVD(P)s – Reference-scaling

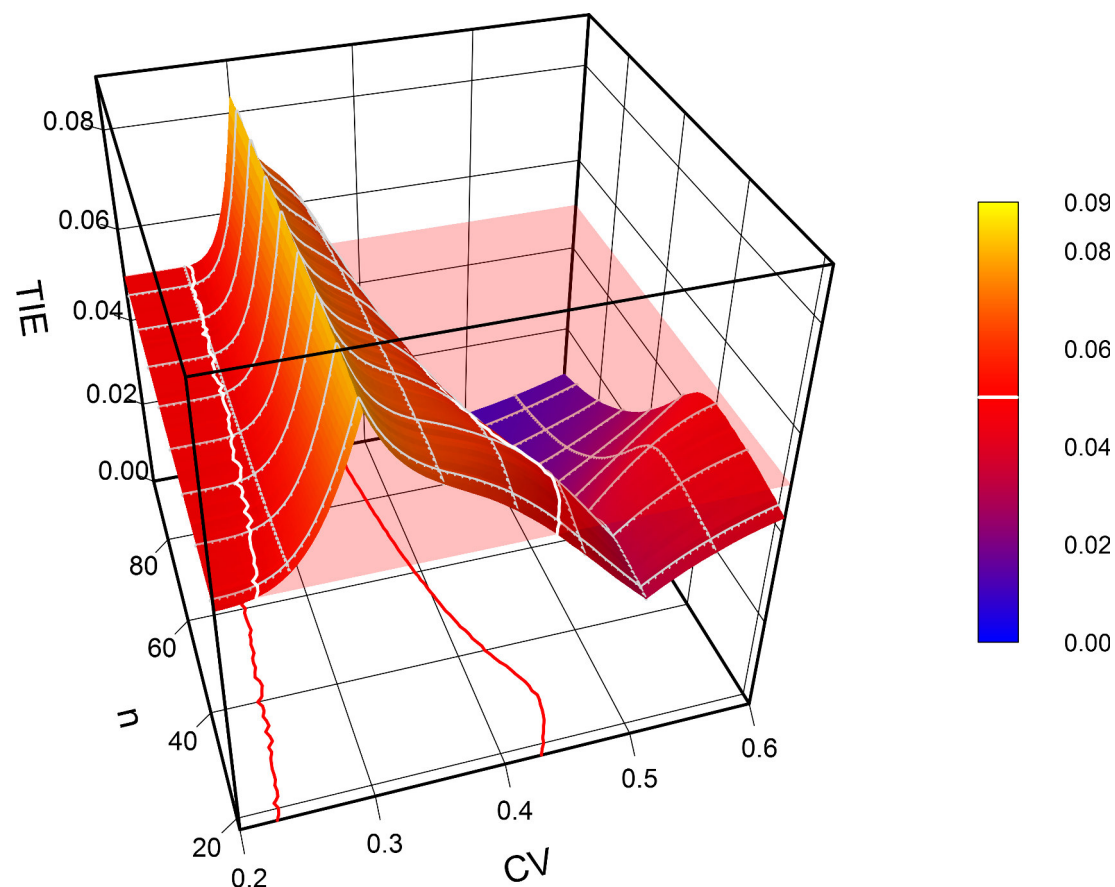
## Assessing the Type I Error (TIE).

- TIE = falsely concluding BE at the limits of the acceptance range.
- Due to the decision scheme direct calculation of the TIE at the scaled limits is not possible;
  - extensive simulations required ( $10^6$  BE studies mandatory).
- Inflation of the TIE suspected.  
(Chow *et al.* 2002, Willavazie and Morgenthien 2006, Chow and Liu 2009, Patterson and Jones 2012).
- Confirmed.
  - EMA's ABEL  
(Tóthfalusi and Endrényi 2009, BEBA-Forum 2013, Wonnemann *et al.* 2015, Muñoz *et al.* 2016, Labes and Schütz 2016).
  - FDA's RSABE  
(Tóthfalusi and Endrényi 2009, BEBA-Forum 2013, Muñoz *et al.* 2016).

# HVD(P)s – Reference-scaling

## Example for ABEL

- RTRT | TRTR  
sample size 18 – 96  
 $CV_{wR}$  20% – 60%
  - $TIE_{max}$  0.0837.
  - Relative increase of the consumer risk 67%!



# HVD(P)s – Reference-scaling

## What is going on here?

- SABE is stated in model *parameters* ...

$$-\theta_S \leq \frac{\mu_T - \mu_R}{\sigma_{wR}} \leq +\theta_S$$

... which are *unknown*.

- Only their *estimates* ( $GMR$ ,  $s_{wR}$ ) are accessible in the actual study.
- At  $CV_{wR}$  30% the decision to scale will be wrong in ~50% of cases.
- If moving away from 30% the chances of a wrong decision decrease and hence, the TIE.
- At high CVs (>43%) both the scaling cap and the *GMR*-restriction help to maintain the TIE <0.05).

# HVD(P)s – Reference-scaling

## Outlook.

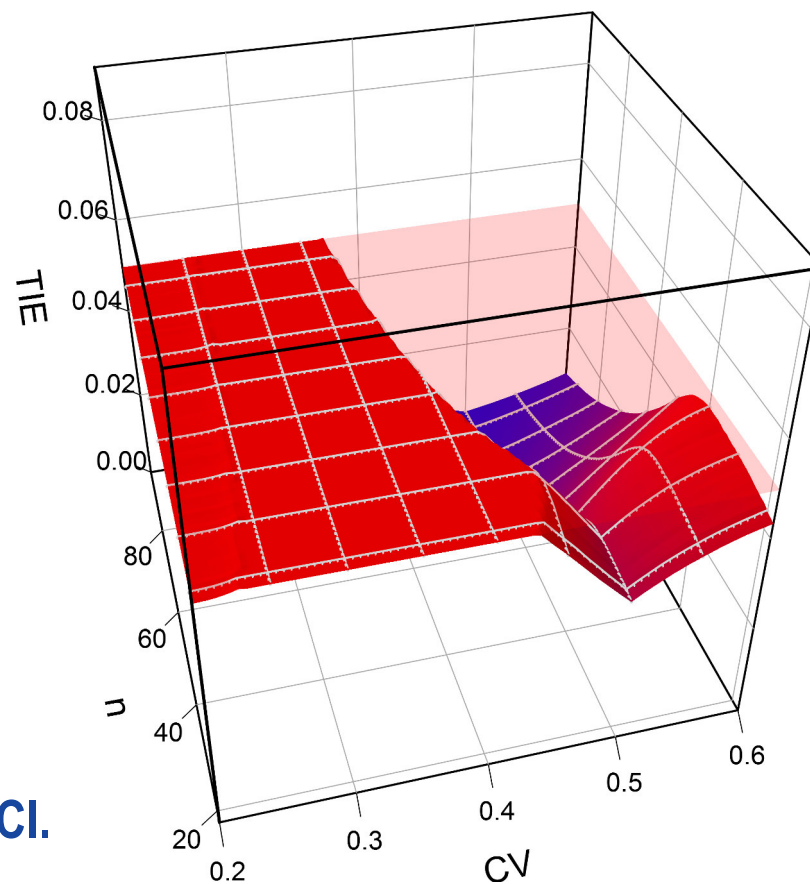
- Utopia
  - Agencies collect  $CV_{wR}$  from submitted studies. Pool them, adjust for designs / degrees of freedom. The EMA publishes a fixed acceptance range in the product-specific guidance. No need for replicate studies any more.  $2 \times 2 \times 2$  cross.overs evaluated by ABE would be sufficient.
- Halfbaked
  - Hope [*sic*] that e.g., Bonferroni preserves the consumer risk. Still apply ABEL, but with a 95% CI ( $\alpha$  0.025).
  - Drawback: Loss of power, substantial increase in sample sizes.
- Proposal
  - Iteratively adjust  $\alpha$  based on the study's  $CV_{wR}$  and sample size – in such a way that the consumer risk is preserved (Labes and Schütz 2016).

Labes D, Schütz H. *Inflation of Type I Error in the Evaluation of Scaled Average Bioequivalence, and a Method for its Control*. Pharm Res. 2016; 33(11): 2805–14. [DOI 10.1007/s11095-016-2006-1](https://doi.org/10.1007/s11095-016-2006-1)

# ABEL (iteratively adjusted $\alpha$ )

## Previous example

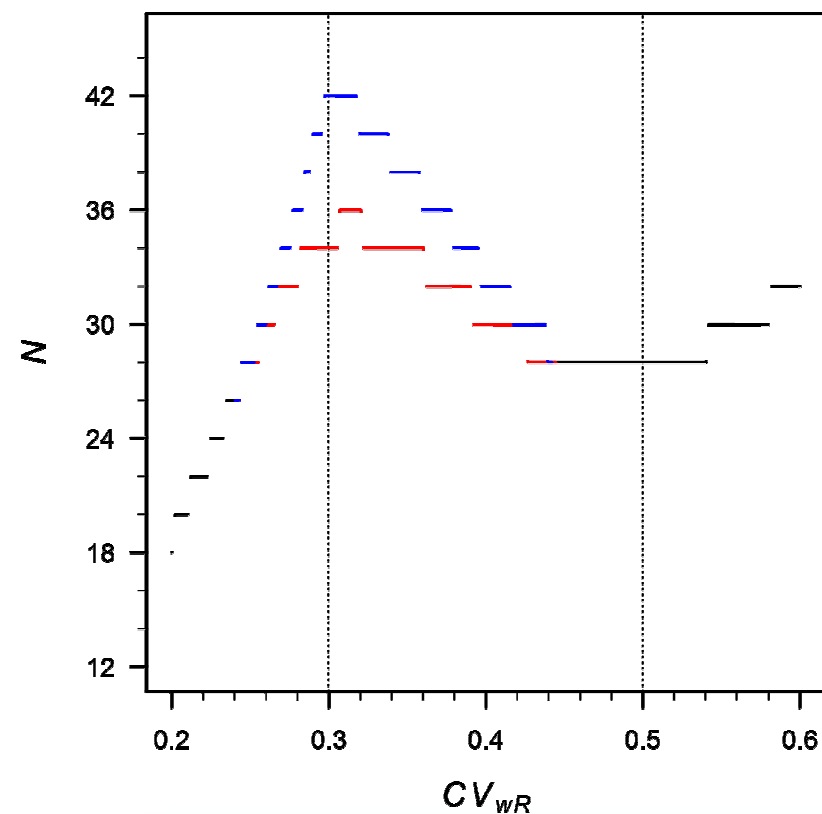
- **Algorithm**
  - Assess the TIE for the nominal  $\alpha$  0.05.
  - If the TIE  $\leq 0.05$ , stop.
  - Otherwise adjust  $\alpha$  (downwards) until the TIE  $\cong 0.05$ .
  - At  $CV_{WR}$  30% (dependent on the sample size)  $\alpha_{adj}$  is 0.0273 – 0.0300;  
→ use a 94.00 – 94.54% CI.



# ABEL (iteratively adjusted $\alpha$ )

## Potential impact on the sample size.

- Example: RTRT | TRTR,  $\theta_0$  0.90, target power 0.80.
  - Moderate in the critical region (— —).
  - $CV_{WR}$  30%: **36** → **42** (+17%);
  - $CV_{WR}$  35%: **34** → **38** (+12%);
  - $CV_{WR}$  40%: **30** → **32** (+7%).
  - None outside (—).



# ABEL (iteratively adjusted $\alpha$ )

**Example (RTRT | TRTR, expected  $CV_{wR}$  35%,  $\theta_0$  0.90, target power 0.80); R package PowerTOST ( $\geq 1.3-3$ ).**

- Estimate the sample size.

```
sampleN.scABEL(CV=0.35, theta0=0.90, targetpower=0.80, design="2x2x4",
               details=FALSE, print=FALSE)[["sample size"]]
[1] 34
```

- Estimate the empiric TIE for this study.

```
UL <- scABEL(CV=0.35)[["upper"]] # scaled limit (1.2948 for CVwR 0.35)
power.scABEL(CV=0.35, theta0=UL, n=34, design="2x2x4", nsims=1e6)
[1] 0.065566
```

- Iteratively adjust  $\alpha$ .

```
scABEL.ad(CV=0.35, n=34, design="2x2x4")
+++++++ scaled (widened) ABEL ++++++
iteratively adjusted alpha
-----
CVwR 0.35, n(i) 17|17 (N 34)
Nominal alpha           : 0.05
Null (true) ratio       : 0.9000
Regulatory settings     : EMA (ABEL)
Empiric TIE for alpha 0.0500 : 0.06557
Power for theta0 0.900   : 0.812
Iteratively adjusted alpha : 0.03630
Empiric TIE for adjusted alpha: 0.05000
Power for theta0 0.900   : 0.773
```

# ABEL (iteratively adjusted $\alpha$ )

- Optionally compensate for the loss in power (0.812  $\rightarrow$  0.773) by increasing the sample size:

```
sampleN.scABEL.ad(CV=0.35, theta0=0.90, targetpower=0.80, design="2x2x4")
+++++++ scaled (widened) ABEL ++++++
          Sample size estimation
          for iteratively adjusted alpha
```

```
-----
Study design: 2x2x4 (RTRT|TRTR)
Expected CVWR 0.35
Nominal alpha      : 0.05
Null (true) ratio  : 0.9000
Target power       : 0.8
Regulatory settings: EMA (ABEL)
Switching CVWR     : 30%
Regulatory constant: 0.760
Expanded limits    : 0.7723...1.2948
Upper scaling cap  : CVWR 0.5
PE constraints     : 0.8000...1.2500
n 38, adj. alpha: 0.03610 (power 0.8100), TIE: 0.05000
```

–  $n$  34  $\rightarrow$  38 (+12%), power 0.773  $\rightarrow$  0.810,  $\alpha_{adj}$  0.0363  $\rightarrow$  0.0361.

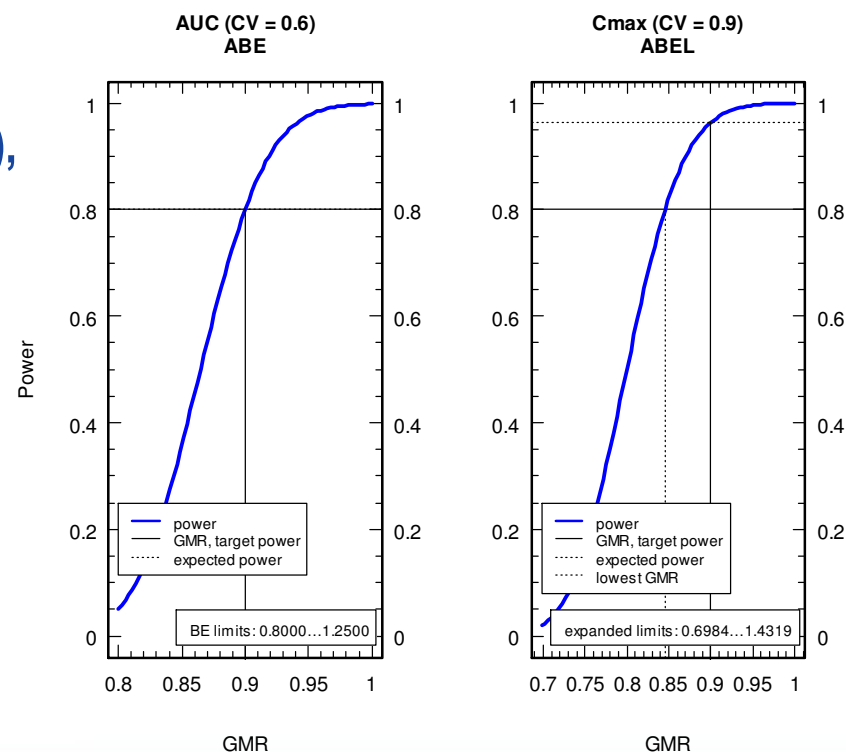


# Side Effect

## Allowing ABEL only for $C_{max}$

- Some drugs show high variability in  $AUC$  as well.
  - Since in such a case the sample size is mandated by  $AUC$ , products with high deviations in  $C_{max}$  will be approved.
  - Example:  $CV_{wR}$  90% ( $C_{max}$ ), 60% ( $AUC$ ),  $\theta_0$  0.90, target power 80% → the study is ‘overpowered’ for  $C_{max}$ ;  $C_{max}$ -GMRs of [0.846 – 1.183] will pass BE. Really desirable?
  - With the FDA’s RSABE the study could be performed in only 34 subjects...

ABEL (EMA): design RTRT|TRTR, target power = 0.8, n = 138 (sample size dependent on AUC)



# NTIDs – tighter BE limits

## EMA (2010)

- In *specific cases* of products with a narrow therapeutic range, the acceptance interval *may* need to be tightened.
  - The acceptance interval for  $AUC$  should be tightened to 90.00 – 111.11%.
  - Where  $C_{max}$  is of particular importance for safety, efficacy or drug level monitoring the 90.00 – 111.11% acceptance interval should also be applied for this parameter.
  - It is not possible to define a set of criteria to categorise drugs as narrow therapeutic index drugs (NTIDs) and it must be decided *case by case* if an active substance is an NTID *based on clinical considerations*.

## EMA (Product-specific guidance 2013 – 2016)

- Sirolimus: 80.00 – 125.00% for  $C_{max}$ , 90.00 – 111.11% for  $AUC_{0-t}$
- Tacrolimus: 80.00 – 125.00% for  $C_{max}$ , 90.00 – 111.11% for  $AUC_{0-72h}$

# NTIDs – tighter BE limits

## Impact of tighter BE limits on sample size

- Example: CV 15%, GMR 0.975, target power 90%, 2×2×2 design.
  - Conventional 80.00 – 125.00%

```
library(PowerTOST)
sampleN.TOST(CV=0.15, theta0=0.975, targetpower=0.90,
             theta1=0.8000, theta2=1.2500,
             print=FALSE)[["Sample size"]]
```

[1] 14

- 90.00 – 111.11%

```
library(PowerTOST)
sampleN.TOST(CV=0.15, theta0=0.975, targetpower=0.90,
             theta1=0.9000, theta2=1.1111,
             print=FALSE)[["Sample size"]]
```

[1] 62

# NTIDs – reference scaling

## FDA

- First recommended in the guidance for warfarin (2012).
  - Scale bioequivalence limits to the variability of the reference product.
  - Compare test and reference product within-subject variability.
  - A fully replicated 4-period study (RTRT | TRTR) is mandatory.
- Scaling approach similar to the FDA's for HVD(P)s.
  - $\sigma_0$  0.10 (CV  $\approx$  10.02505%)
  - $\Delta$  1.11111
- Must demonstrate:
  - BE with the scaled approach.
  - BE with the conventional limits.
  - Variance of T not higher than of R (upper 90% CI of  $\sigma_{wT} / \sigma_{wR} \leq 2.5$ )

# NTIDs – sample sizes

**GMR 0.975,  $CV_{wT} = CV_{wR}$ , target power 90%, 2×2×4 design.**

$CV_{wR}$	90.00 – 111.11%	RSABE
	EMA	FDA
	$n$	
5.0	12*	44
7.5	12*	26
10.0	14	22
12.5	22	20
15.0	32	20
20.0	54	18

**As above;  $CV_{wT} = 1.5 \times CV_{wR}$ , FDA's RSABE**

$CV_{wR}$	$CV_{wT}$	$n$
5.0	7.50	48
7.5	11.25	36
10.0	15.00	32
12.5	18.75	30
15.0	22.50	30
20.0	30.00	28

# Establishing the Biostudy Statistical Design

**Thank You!**  
*Open Questions?*



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